

# **“What do dynamical calculations of birch trunk deformation & breaking, and of the flight of the detached wing fragment tell us about the catastrophe of flight PLF 101 in Smolensk”**

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University of Toronto



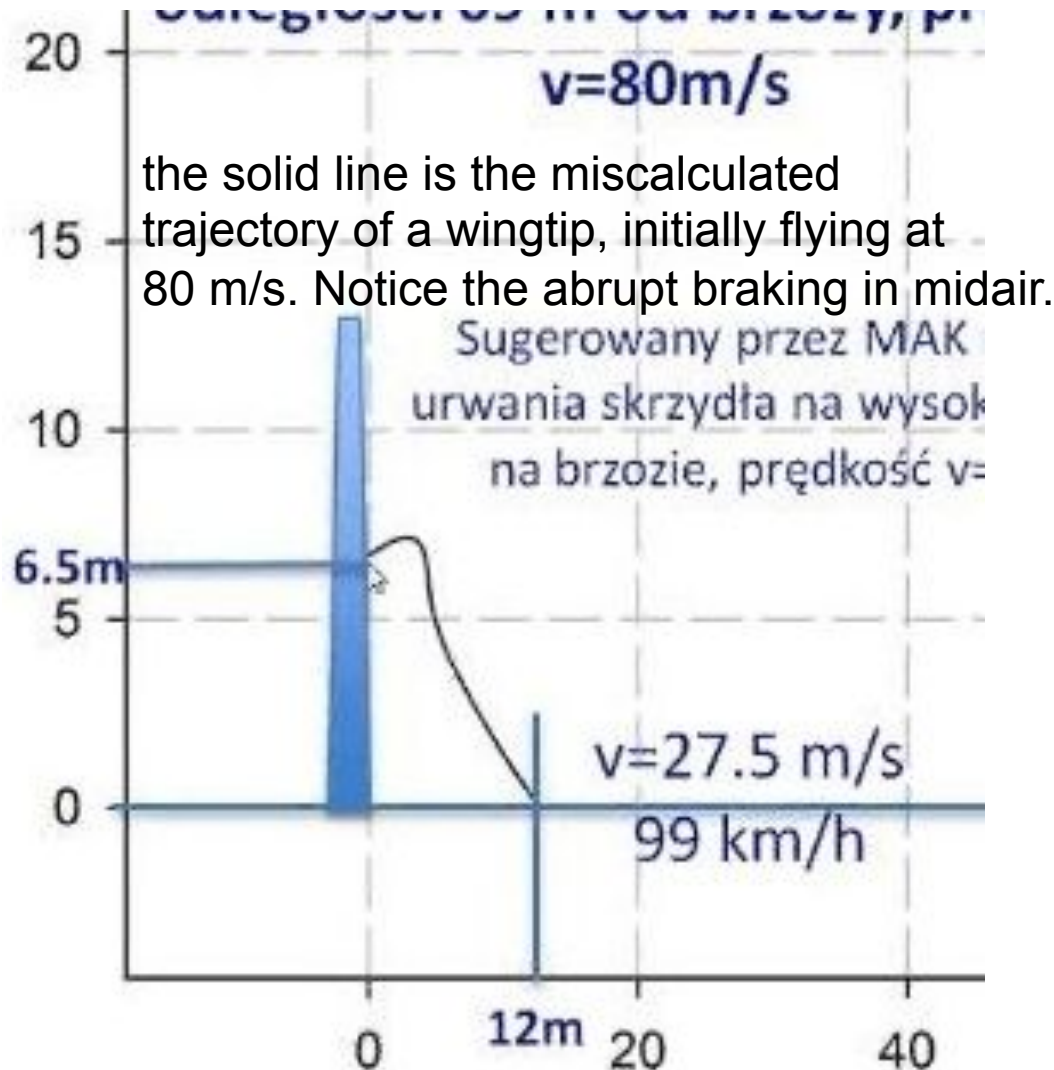
# TOPICS

- Where and when was the wintip of TU-154M detached from the aircraft?
- How was it moving and how far did it fly?
- Where did the fatal half-roll of flight PLF 101 begin?
- What was happening with the birch tree during the collision? Did the wingtip separate from the aircraft or cut the this birch and remain attached to the rest of the wing?



# Incorrect calculations of Dr. Binienda et al. (2012)

Hypothesis of a 10-12 meter flight with sudden, unexplained braking in mid-air.



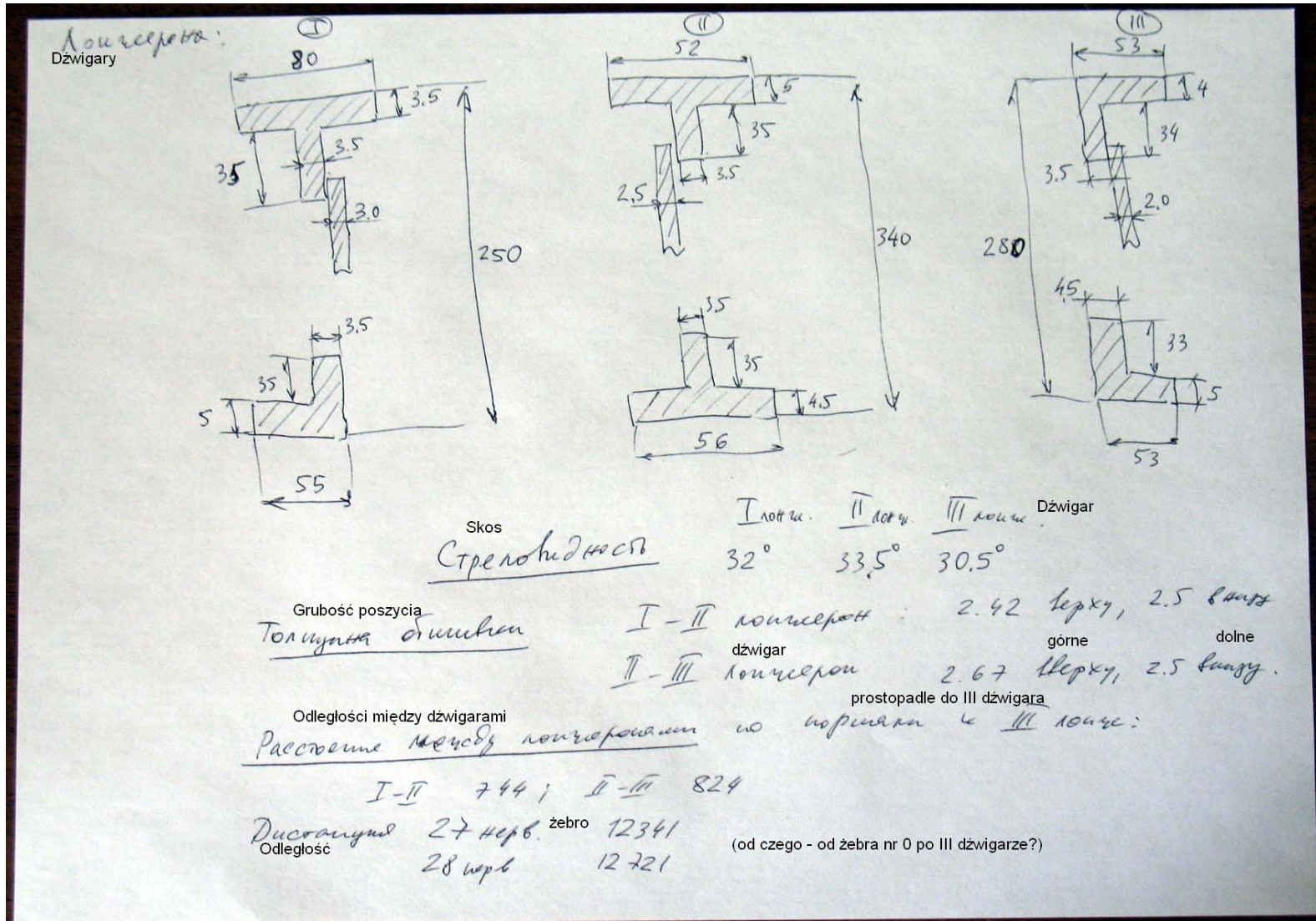
Such a scenario requires: either a deceleration in air reaching the value of 60 g, i.e. coefficient of drag  $C_d \sim 20\text{-}30$ , or air density 20-30 times higher than actual, the mass of the wing too low 20x, or (quite likely!) the Reynolds number  $Re$  in model orders of magnitude too low as a consequence of low resolution or otherwise wrong numerical calculations).

Pick your favorite reason – Binienda's calculations are wrong in any case.





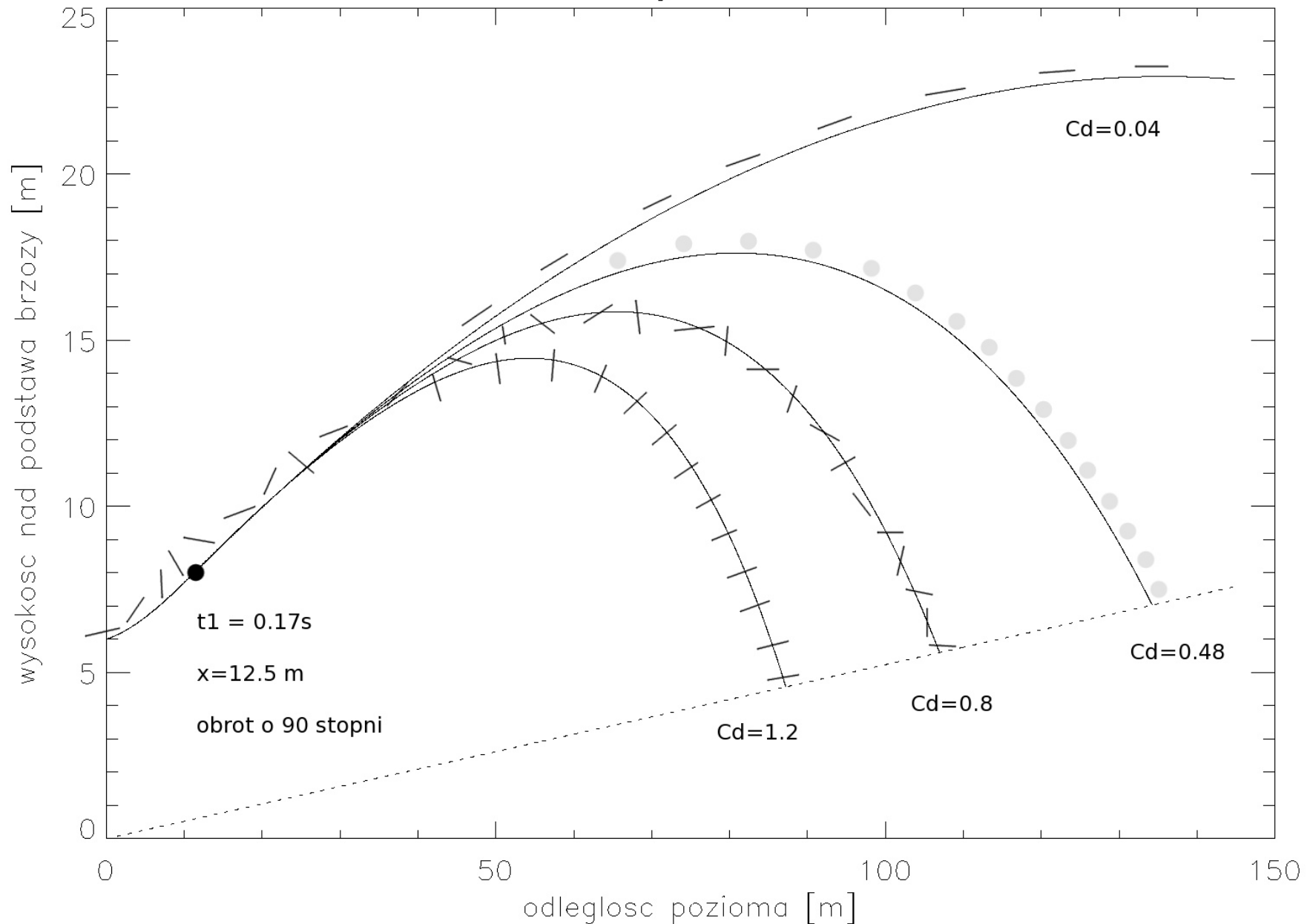
Binienda (2012) did FEM analysis of wing-tree collision. He did not know either the true thicknesses of aluminum alloy sheets (D16) or even the correct range in which they should lie. His models had metal 5-12 mm thick, which is 3-4 times too high. We now know the dimensions directly from Tupolev design bureau. Every engineer should be able to estimate the required thickness for transport aircraft to  $\pm 20\%$  accuracy.





# My results for flightpath of a wingtip in 2012

trajektorie



However, I recently added detailed consideration of unsteady aerodynamics, where lift and drag forces up to a few times higher than in the stabilized flow are possible.

*J. Fluid Mech.* (1979), vol. 92, part 2, pp. 327–348

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*Printed in Great Britain*

## **Autorotating flat-plate wings: the effect of the moment of inertia, geometry and Reynolds number**

**By J. D. IVERSEN**

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(Received 2 November 1977)

Free-flight and wind-tunnel measurements by previous investigators of the flat-plate autorotation phenomenon have been analysed. The variation of the autorotation characteristics with changes in the Reynolds number and the aspect ratio, thickness ratio and moment of inertia of the flat plate have been correlated. The interpretation of the role of the Reynolds number made in a previous investigation is shown to be incorrect. The tip-speed ratio, for the ranges of the dimensionless parameters investigated, is shown to be a function of only the plate aspect ratio, thickness ratio, and also the moment of inertia if the latter is sufficiently small. The lift and drag coefficients, and therefore the free-flight glide angle, are shown to be functions of the tip-speed ratio, the aspect ratio and the Reynolds numbers based on the chord and plate thickness.

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### **1. The Magnus rotor: introduction**

The Magnus rotor as defined here is a cylinder of arbitrary cross-section which revolves about an axis perpendicular to the cross-section and moves through air or another fluid in a direction perpendicular to this axis (or is stationed in a wind tunnel

## **JFM RAPIDS** [journals.cambridge.org/rapids](http://journals.cambridge.org/rapids)

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### **Unsteady pitching flat plates**

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Direct force measurements and qualitative flow visualization were used to compare flow field evolution versus lift and drag for a nominally two-dimensional rigid flat plate executing smoothed linear pitch ramp manoeuvres in a water tunnel. Non-dimensional pitch rate was varied from 0.01 to 0.5, incidence angle from 0 to 90°, and pitch pivot point from the leading to the trailing edge. For low pitch rates, the main unsteady effect is delay of stall beyond the steady incidence angle. Shifting the time base to account for different pivot points leads to collapse of both lift/drag history and flow field history. For higher rates, a leading edge vortex forms; its history also depends on pitch pivot point, but linear shift in time base is not successful in collapsing lift/drag history. Instead, a phenomenological algebraic relation, valid at the higher pitch rates, accounts for lift and drag for different rates and pivot points, through at least 45° incidence angle.



## Aerodynamic Characterisation of Static and Auto-rotating plates using coupled CFD-RBD simulations

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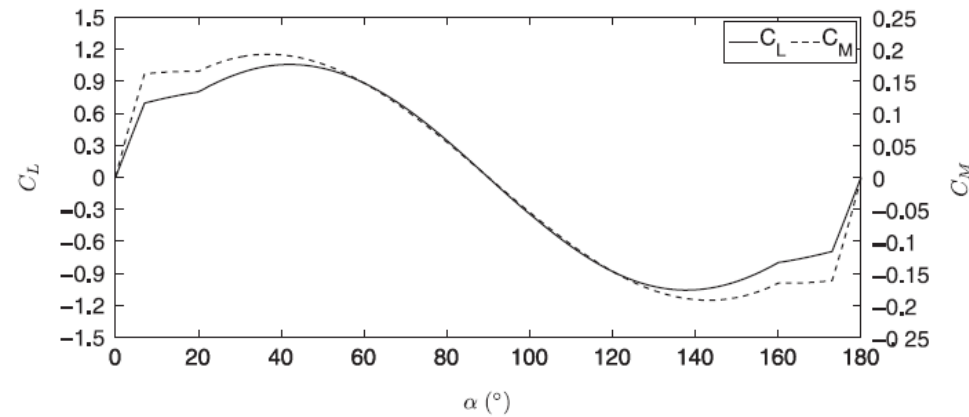
<sup>c</sup> *Associate Professor, Department of Civil Engineering,  
University of Nottingham, UK, [john.owen@nottingham.ac.uk](mailto:john.owen@nottingham.ac.uk)*

**ABSTRACT:** The phenomenon of plate autorotation is one that has application in a number of practical problems. Previous experimental investigations of autorotation have however been focused on single degree of freedom autorotation about a fixed axis due to the practical difficulties involved with implementing full 3D autorotation. Numerical studies of the problem have also focused mainly on 2D and low Reynolds number problems with one rotational degree of freedom. However in many practical situations, autorotation is three-dimensional in nature, exhibiting non-linear three degree of rotational freedom autorotation about an arbitrary axis. A more complete numerical treatment of autorotation is therefore necessary. This paper presents a three-degree of freedom simulation of the autorotation of a 3D low aspect ratio plate about its centre of mass in a high Reynolds number flow using a coupled CFD-RBD approach. The effects of vortex shedding on plate motion are found to be negligible and the autorotation phenomenon is found to be strongly dependent on the initial orientation of the plate. Predicted autorotational velocities are found to agree with experimentally derived correlation expressions.

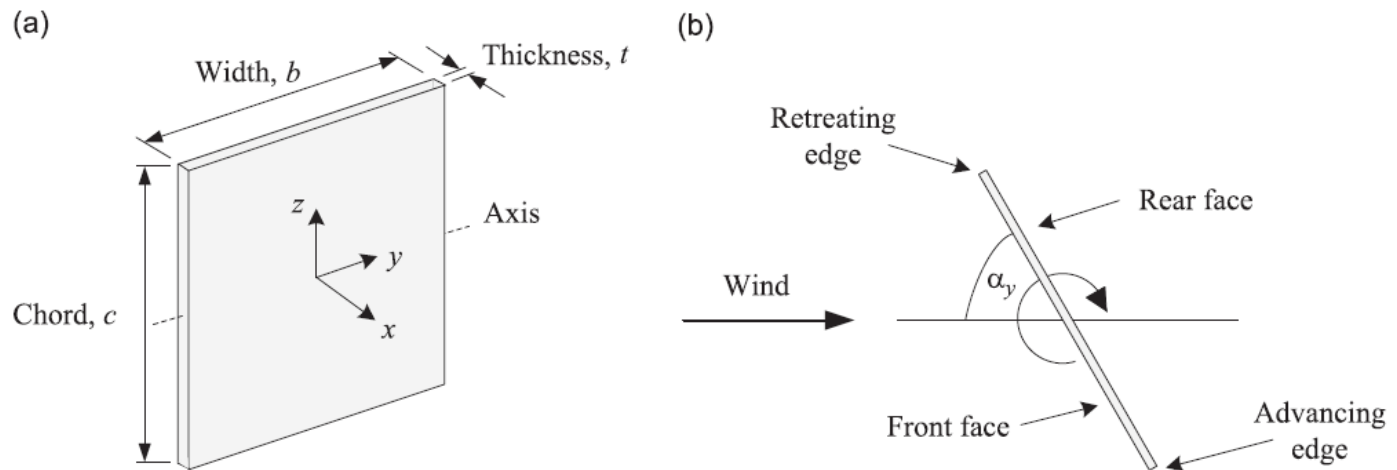
The autorotation occurs at AR (elongation factors) in a wide range, for instance in case of flat square pieces. The phenomenon is insensitive to Reynolds number  $Re$ .

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*D.M. Hargreaves et al. / Journal of Fluids and Structures 46 (2014) 111–133*

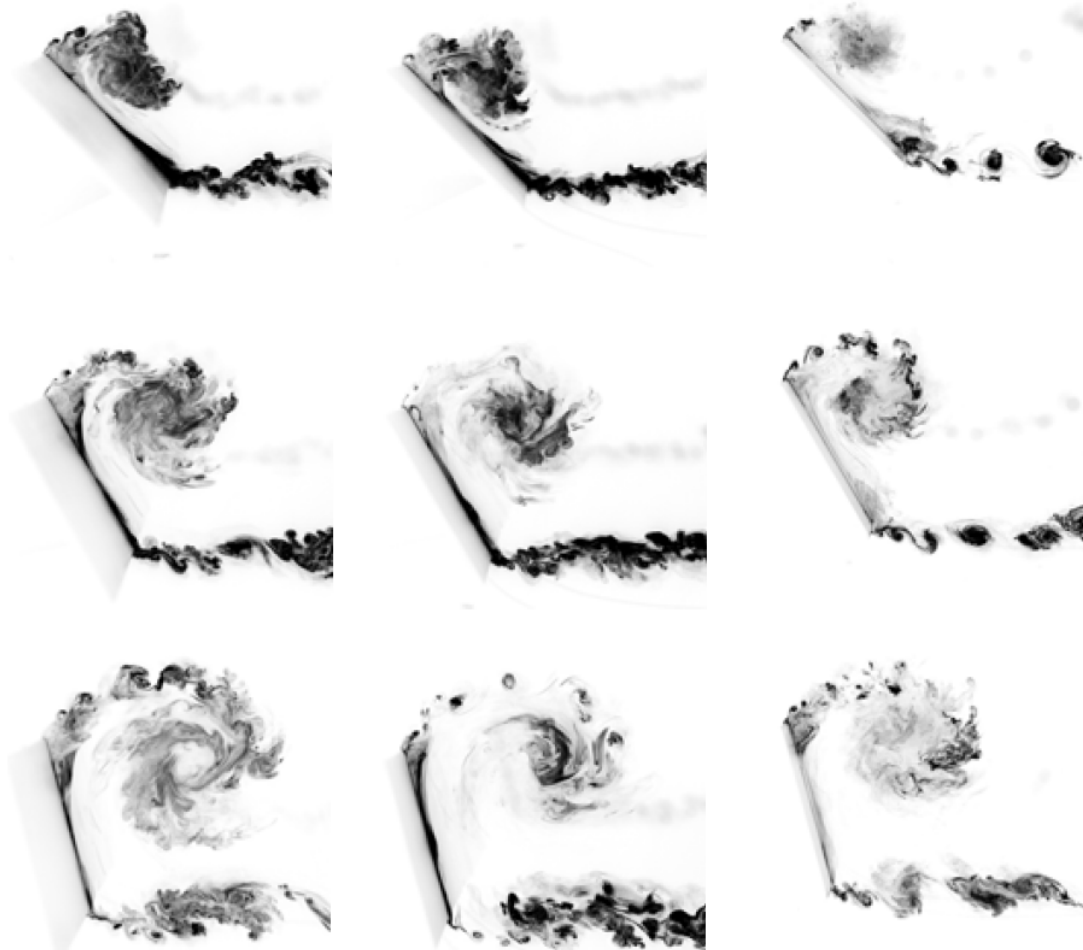


**Fig. 1.** Steady-state curves showing the variation of lift,  $C_L$ , and moment,  $C_M$ , coefficients with angle of attack,  $\alpha$  for static square flat plates held in a steady flow (ESDU, 1970).



**Fig. 2.** (a) Dimensions and orientation of the plate and (b) the nomenclature associated with an autorotating plate.

Non-stationary airfoil aerodynamics;  
Autorotation is caused by a lowered pressure of the vortex  
behind the leading edge. Autorotation prefers a speed of  
rotation such that the linear rotation speed of the edge equals  
0.35-0.5 of the speed of the undisturbed, incoming airflow





example of detailed calculation

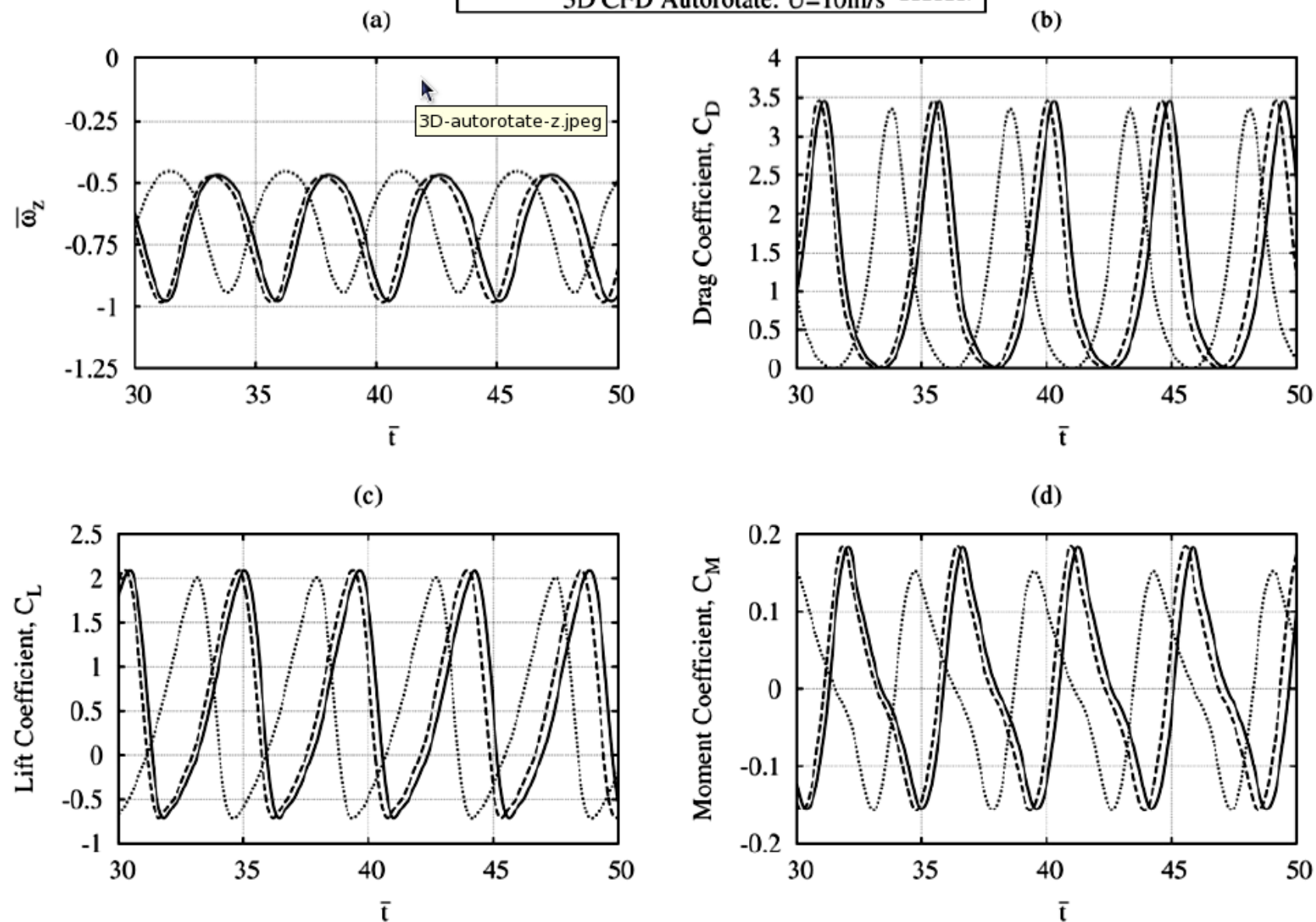
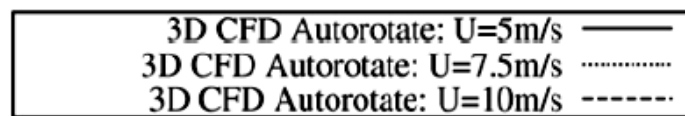


Figure 5: Time series plots for autorotational speed (a), drag coefficients (b), lift coefficients (c) and moment coefficients (d), obtained from 3D CFD-RBD simulations performed at various wind speeds

# Free flight of the plate: rotation around the long axis with nutation

## 4.3 Free-Axis Autorotation

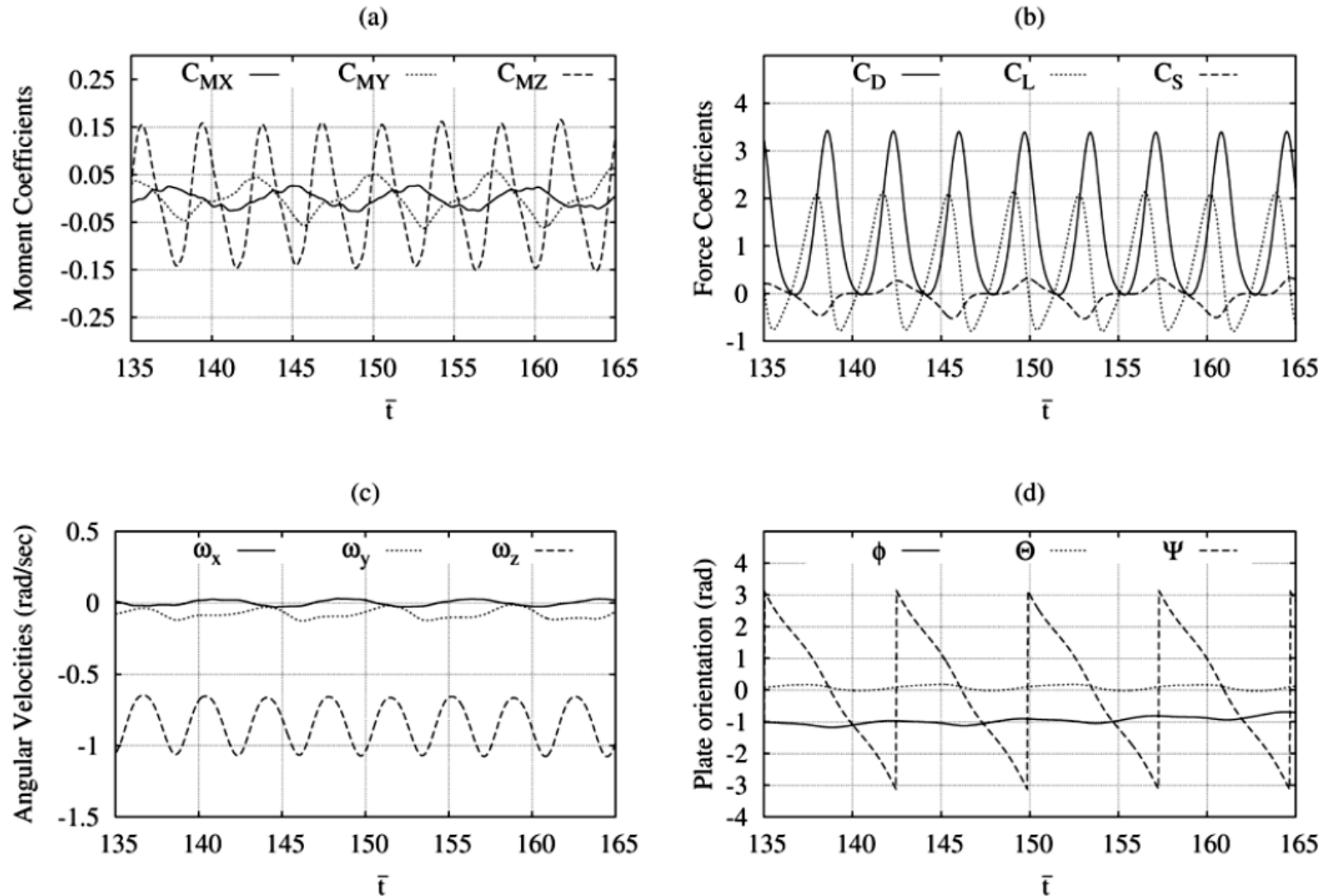
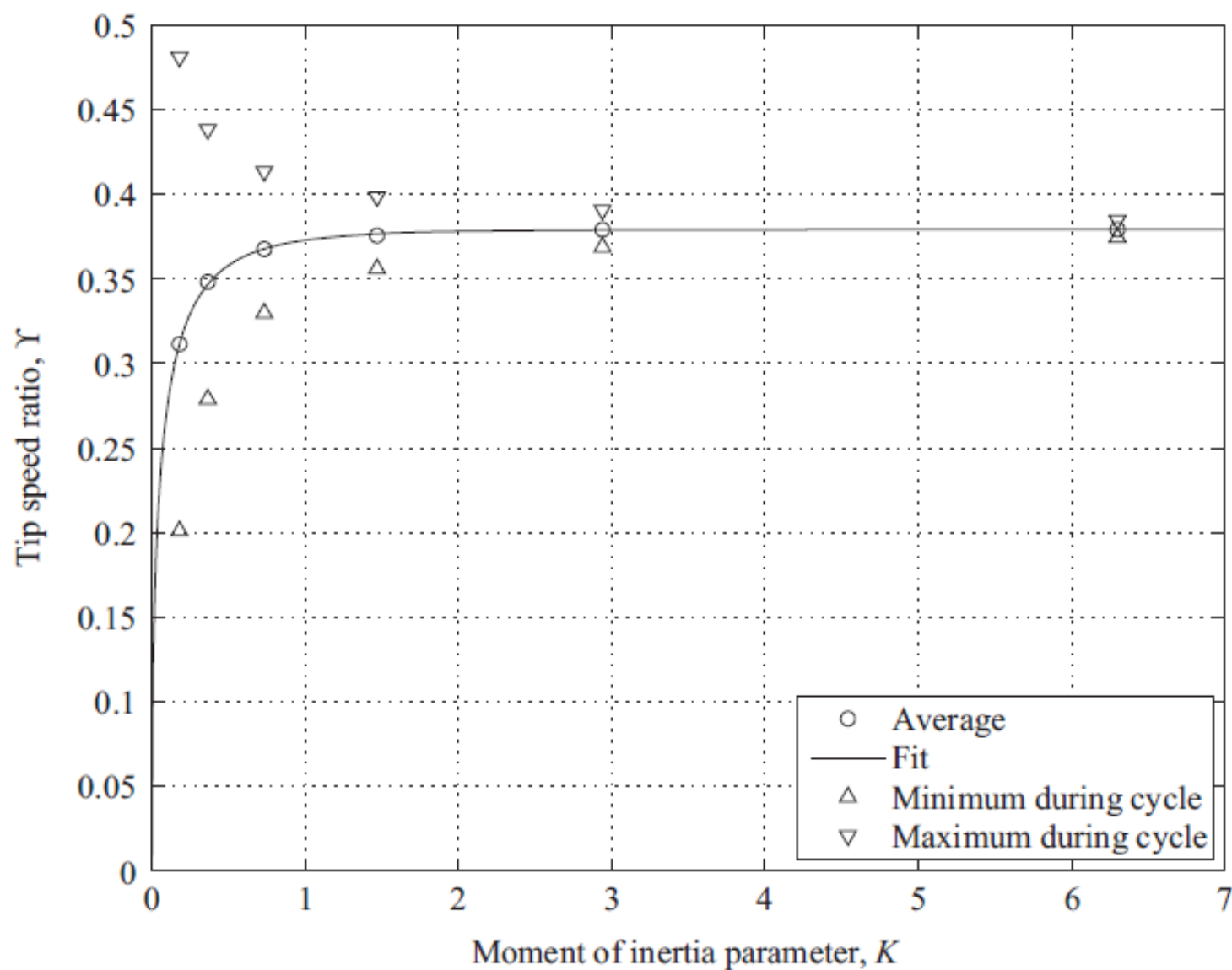
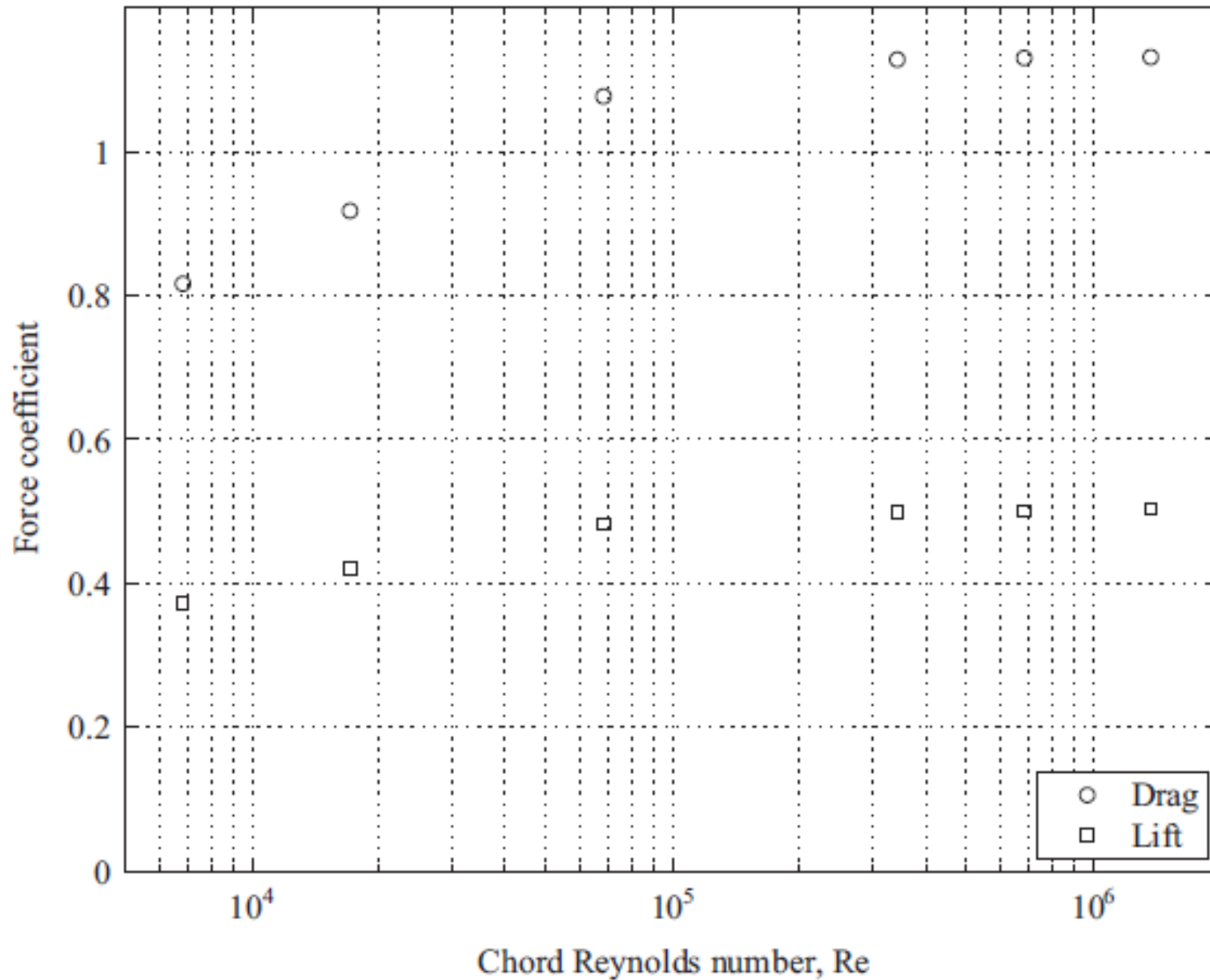


Figure 7: Moments (a), Forces (b), Angular velocities (c) and Orientation (d) from CFD-RBD simulations of a plate autorotating freely about an arbitrary axis through its centre of mass.





unsteady flow results in lift force insensitive to viscosity (Re number)





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## Journal of Fluids and Structures

journal homepage: [www.elsevier.com/locate/jfs](http://www.elsevier.com/locate/jfs)

# The computational fluid dynamics modelling of the autorotation of square, flat plates



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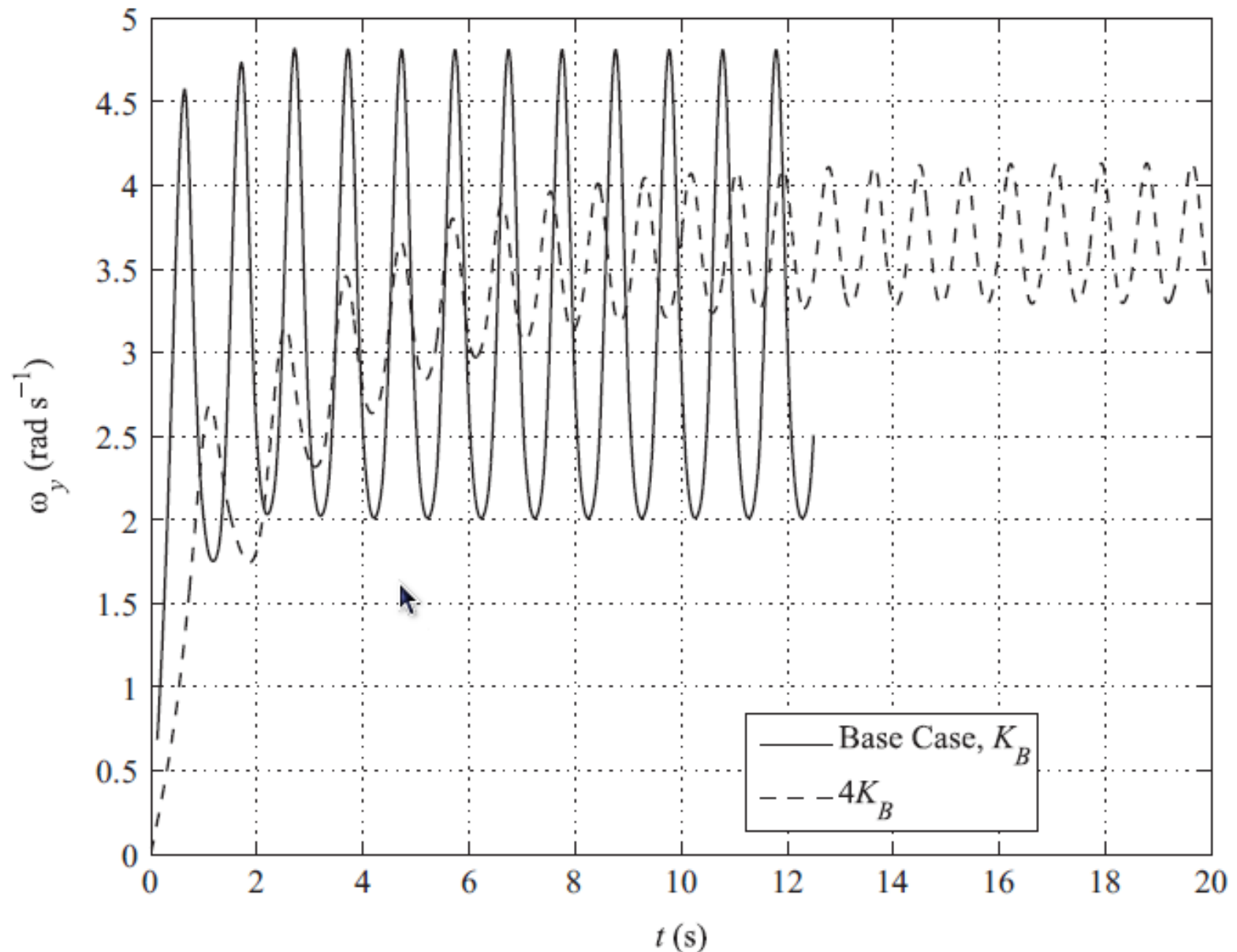
Fluid–structure interaction

## ABSTRACT

This paper examines the use of a coupled Computational Fluid Dynamics (CFD) – Rigid Body Dynamics (RBD) model to study the fixed-axis autorotation of a square flat plate. The calibration of the model against existing wind tunnel data is described. During the calibration, the CFD models were able to identify complex period autorotation rates, which were attributable to a mass eccentricity in the experimental plate. The predicted flow fields around the autorotating plates are found to be consistent with existing observations. In addition, the pressure coefficients from the wind tunnel and computational work were found to be in good agreement. By comparing these pressure distributions and the vortex shedding patterns at various stages through an autorotation cycle, it was possible to gain important insights into the flow structures that evolve around the plate. The CFD model is also compared against existing correlation functions that relate the mean tip speed ratio of the plate to the aspect ratio, thickness ratio and mass moment of inertia of the plate. Agreement is found to be good for aspect ratios of 1, but poor away from this value. However, other aspects of the numerical modelling are consistent with the correlations.

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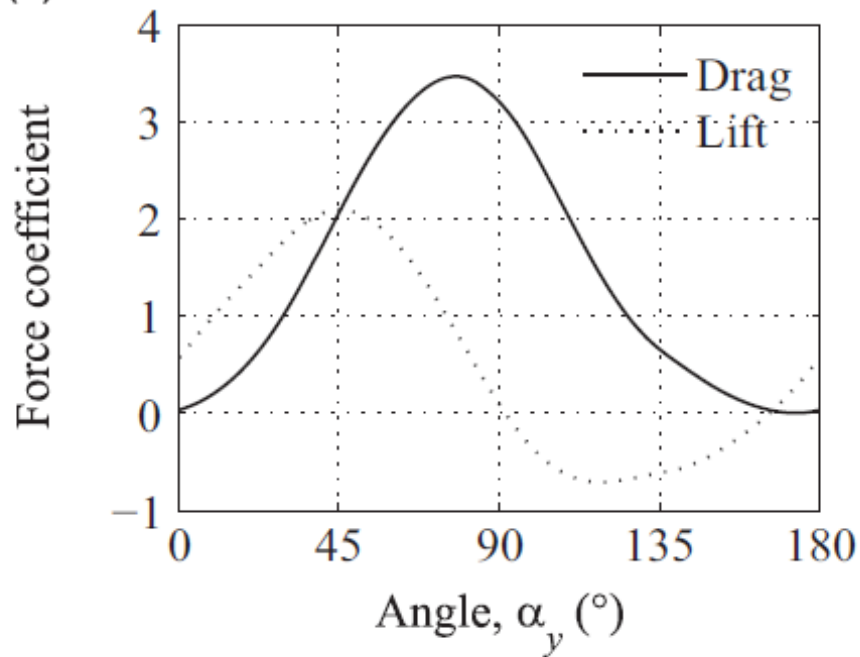
The dashed line shows a slow stabilization of rotation rate after many full turns for a dimensionless coefficient of the moment of inertia appropriate for the detached wingtip of PLF 101 (timescale, however, relates to a different, published model)



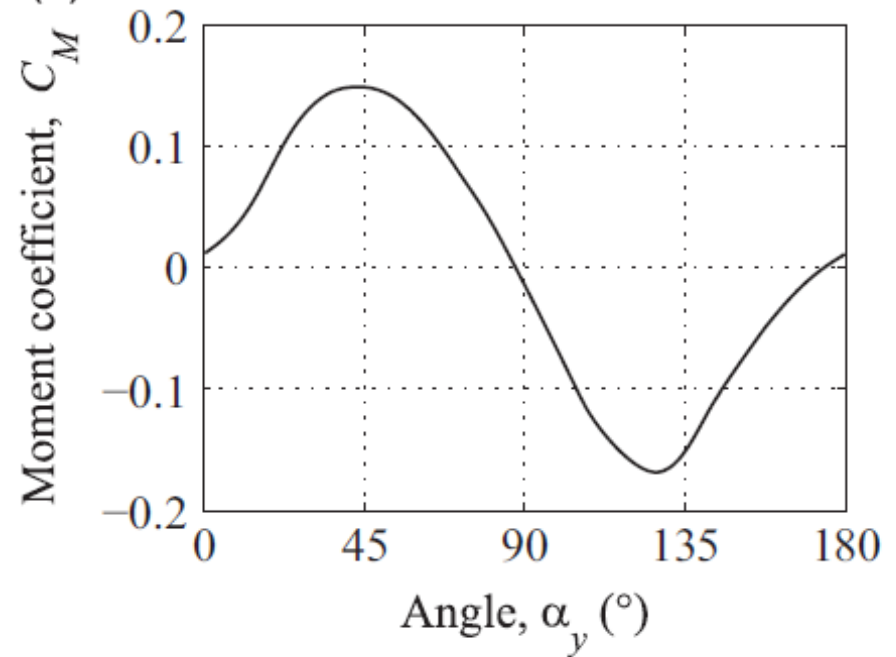


# Cd, CL and Cm as a function of the angle of attack of autorotating airfoil

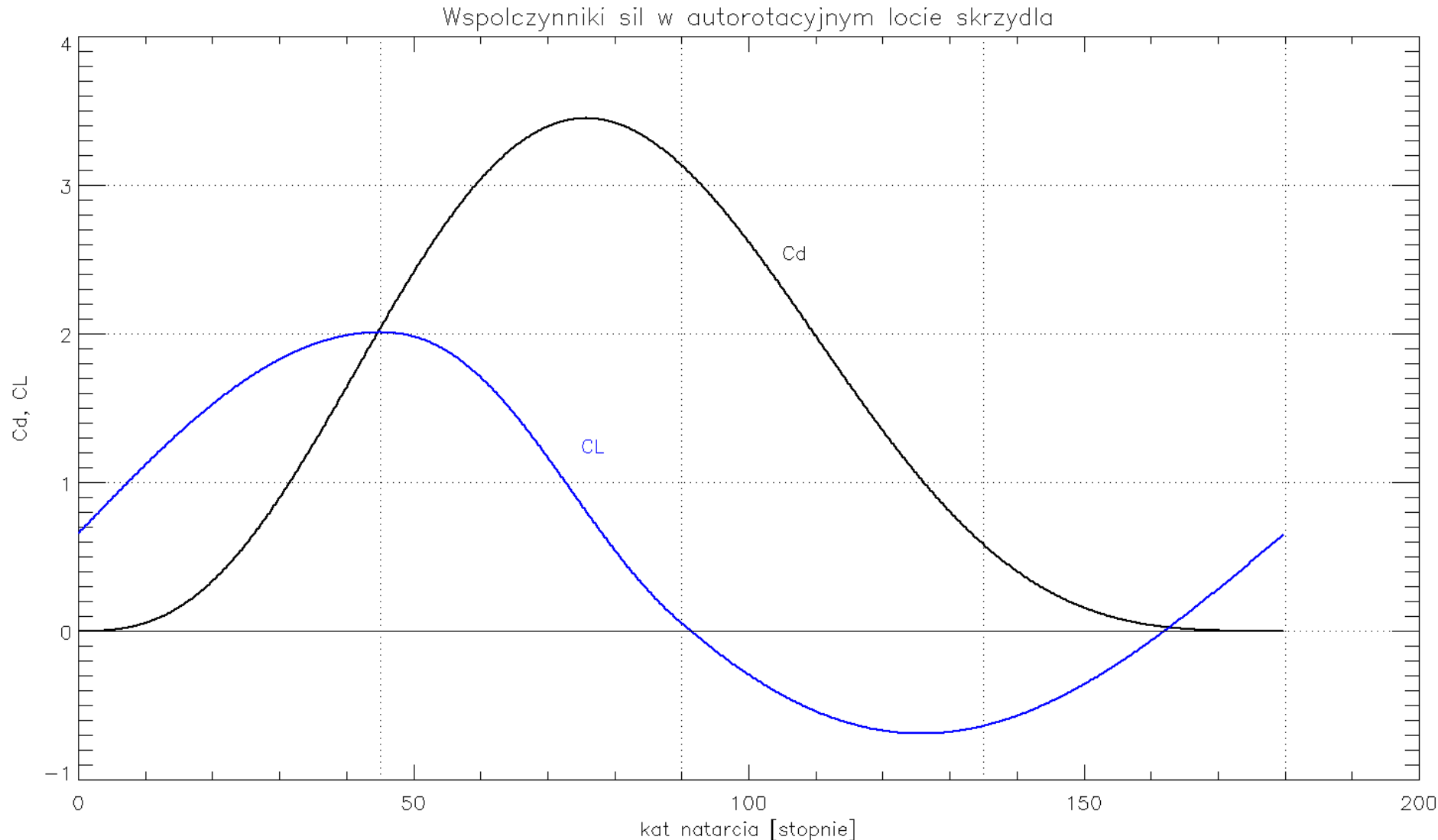
(c)



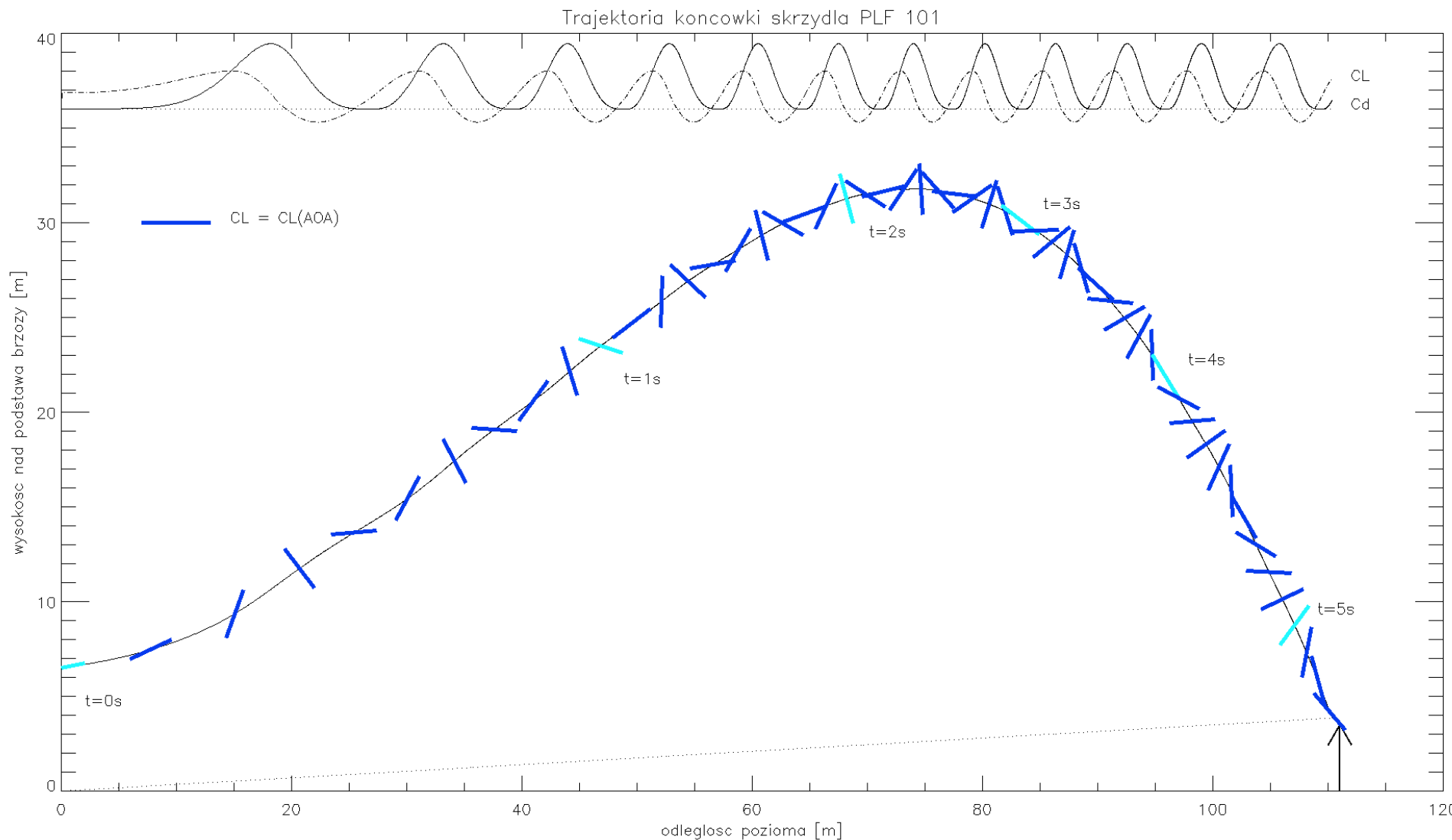
(d)



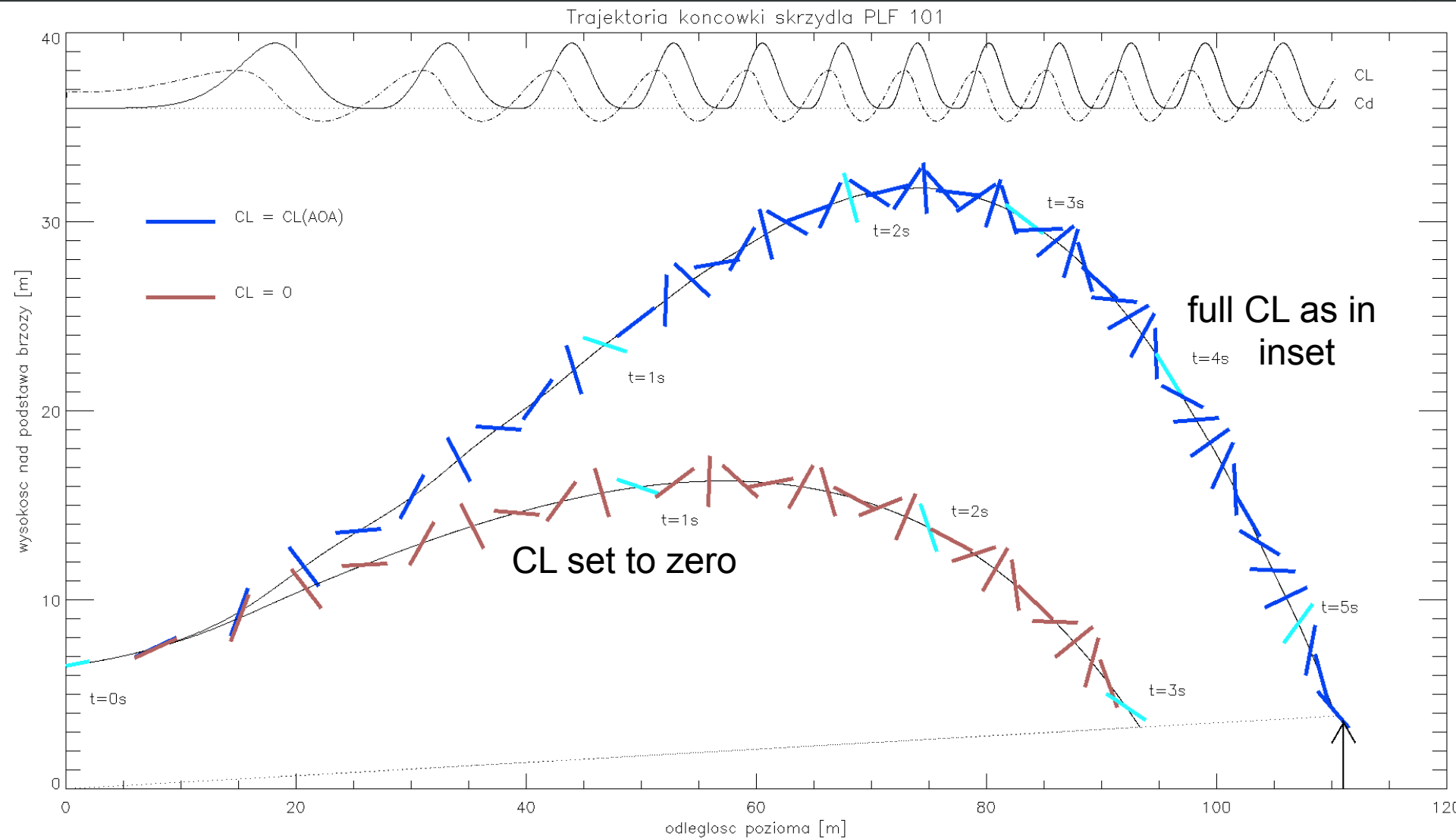
# CL and Cd coefficients (as a function of the angle of attack) during autorotation of the wingtip of Tupolev PLF 101



# Numerical trajectory and the rotation of the wingtip, taking into account autorotation, drag force and the Magnus (lift) force



# Comparison of flight with and without Magnus' effect





# Conclusions about the wingtip trajectory: the wingtip:

- rapidly accelerated up and began autorotating
- It flew for about 5 seconds, rotating along its long axis with some nutation
- It fell after covering about 110 m distance with velocity not larger than  $\sim 70$  km/h, at a  $\sim 50$  degrees angle to the horizon
- Agreement with the reality as found by post-accident investigations is very good.

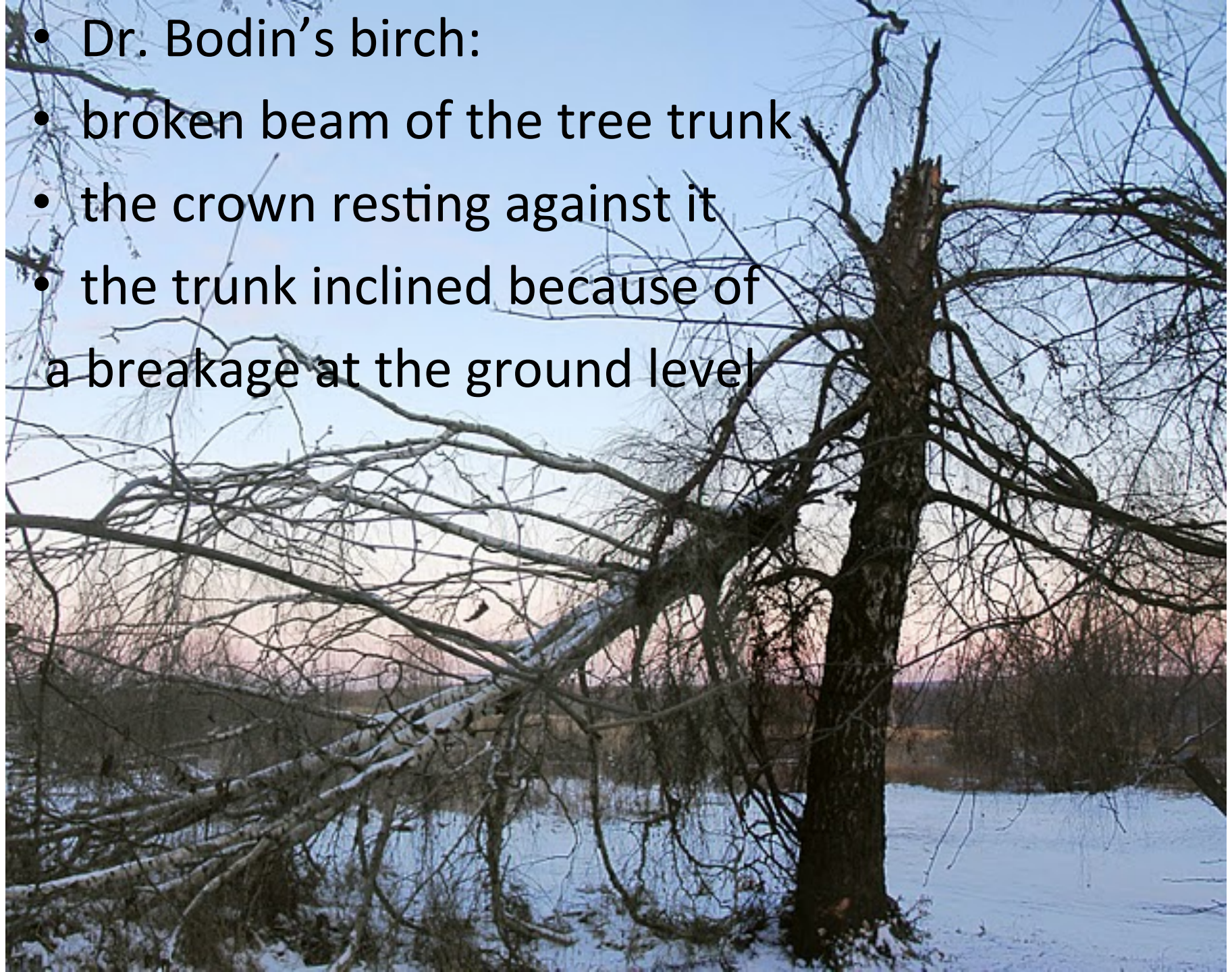
Part II of the presentation:

# How was the outer part of the wing detached?





- Dr. Bodin's birch:
- broken beam of the tree trunk
- the crown resting against it
- the trunk inclined because of a breakage at the ground level





# Facts about Bodin's birch:

*no missing sector of a trunk*, potentially crushed by a wing. In 2012 the military prosecutor's office physically reconstructed most of the beam of the birch from the broken parts, which fit together without much timber loss.



Tree trunk after collision has up to 1 m-long splinters. It was not cut or crushed sector-wise, but broken at moderate speed. The position of the tree top shows the direction of collision that has bent the birch beyond the modulus of rupture (MOR) of fibers. The tree was dynamically hit in by a slanted wing of west-moving aircraft.



# Trunk's inclination







.is due to a split  
(breakage)  
at its bottom, on the  
side from which the  
tree was hit.

.

The double breakage  
on opposite sides of  
the trunk are a sure  
sign of a dynamic  
bending

# Typical data about the wood



Pergamon

*Int. J. Impact Engng.*, Vol. 19, Nos. 5-6, pp. 531-570, 1997

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## DYNAMIC UNIAxIAL CRUSHING OF WOOD

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*(Received 30 October 1996; in revised form 30 January 1997)*

## EXPERIMENTAL RESULTS

### *Mechanical properties at the static loading.*

The testing of wood under static loading in tension, pressure and in bending represents a standard procedure. Owing to this fact, no description of these experiments is presented. The results of this testing are given in Table 1.

Table 1. Strengths of the tested woods. (ME – modulus of elasticity in MPa, MR – modulus of rupture in MPa)

WOOD	Density (kg/m <sup>3</sup> )	Strength in tension    (MPa)	Strength in tension ⊥ (MPa)	Strength in pressure    (MPa)	Strength in pressure ⊥ (MPa)	MR	ME	Tough ness J/cm <sup>2</sup>
Spruce	440	84	1.5	30	4.1	60	9 100	4.9
Pine	530	102	2.9	54	7.5	98	11 750	6.9
Oak	700	108	3.3	42	11.5	116	11 600	7.4
Beech	720	130	3.5	46	7.5	104	13 100	7.8
Birch	730	134	6.9	50	10.8	134	16 100	6.6



Table 1. Numbers of specimens measured ( $N$ ), means, standard deviations and the outermost values for the specific gravity ( $\rho_{12}$ ), MOE and MOR for *Betula pendula* and *B. pubescens*. Below the Pearson correlations between the study variables by species

Species ( $N$ )	<i>B. pendula</i> (249)			<i>B. pubescens</i> (361)		
	$\rho_{12}$	MOE, GPa	MOR, MPa	$\rho_{12}$	MOE, GPa	MOR, MPa
Mean	565.9	14.5	113.9	538.1	13.2	104.1
Std. deviation	38.7	2.1	14.8	35.7	1.9	14.1
Min	440.1	7.8	69.8	456.9	8.2	61.3
Max	687.3	19.9	156.6	640.8	20.0	141.4
Pearson correlations						
$\rho_{12}$	1.000			1.000		
MOE, GPa	0.694	1.000		0.663	1.000	
MOR, MPa	0.827	0.877	1.000	0.792	0.860	1.000

Table 2. Bending properties of birch wood, species combined. A comparison of the means of the current study with those presented in the literature

Characteristics	Current study	Jalava (1945)	Wagenführ (1996)	Dunham et al. (1999)	
	Small clears	Small clears	Small clears	Small clears	Sawn wood
MOE, GPa	13.7	14.1–15.4	14.5–16.5	8.5–14.0	8.2–13.2
MOR, MPa	108.1	98.6–110.9	76–155	93.1–132.3	46.6–64.3

# Behavior of wood under tension (modulus of rupture MOR) vs. compression

*S. Holmberg et al. / Computers and Electronics in Agriculture*

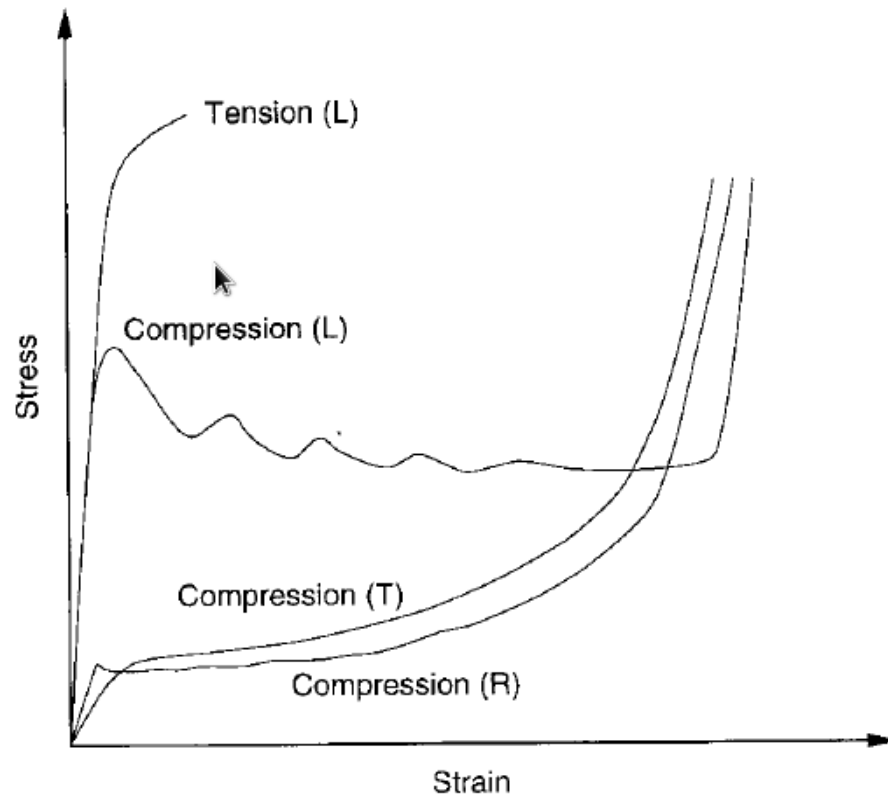
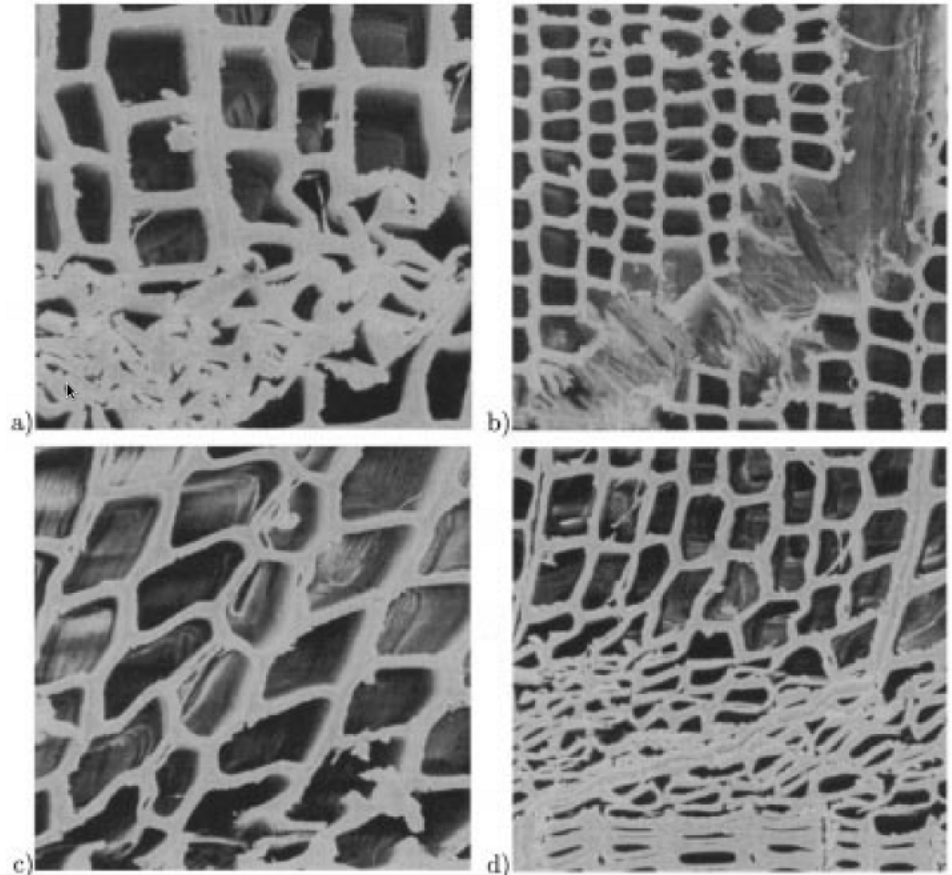


Fig. 9. Typical stress–strain curves for wood loaded in compression in the longitudinal, radial and tangential directions and for tension in the longitudinal direction.

Wood cells were being crushed following the first contact with the wing. About 15 percent of the trunk sector was crushed by the wing. Afterwards, the contact area grew and the stress values dropped below the timber crushing limit. The tree meanwhile started being deflected as a whole and the wing started fragmenting after buckling and exceeding locally the metal yield stress.



# Estimates of birch wood and oak strengths

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S.R. Reid and C. Peng

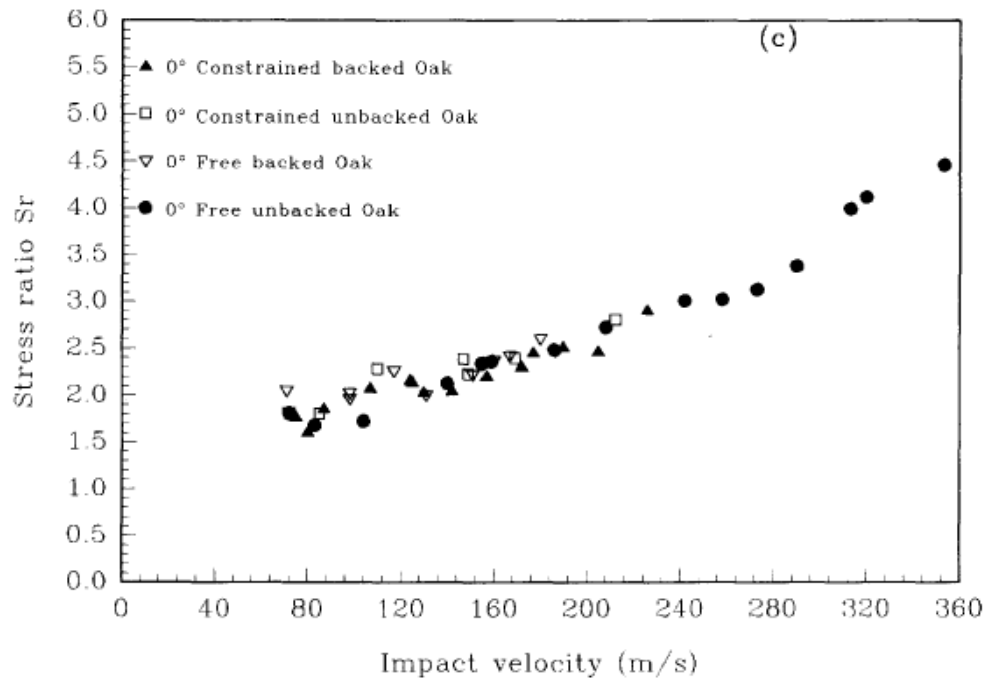
Table 1. Uniaxial quasi-static parameters for wood specimens tested under laterally constrained conditions (uniaxial compression); 75 mm diameter  $\times$  75 mm high

Wood and grain orientation	Initial density, $\rho_0$ (kg m <sup>-3</sup> )	Initial crush stress, $\sigma_{cr}$ (N mm <sup>-2</sup> )	Theoretical crush stress, Eqns (1) or (2) (N mm <sup>-2</sup> )	Locking strain, $\epsilon_l$	Specific locking energy (kJ kg <sup>-1</sup> )
Balsa 0°	277	27.0	27.7	0.68	63.4
Balsa 90°	264	1.6	2.2	0.65	10
Y. Pine 0°	383	43.3	38.3	0.64	62.2
Y. Pine 90°	396	5.1	4.9	0.60	15.2
Redwood 0°	367	43.0	36.7	0.65	59.0
Redwood 90°	409	10.5	5.2	0.58	16.3
A. Oak 0°	725	75.0	72.5	0.33	30.4
A. Oak 90°	695	12.3	15.0	0.37	16.0
Ekki 90°*	1051	24.0	34.4	—	—
Ekki 90°	1183	18.2	43.5	0.13	3.7

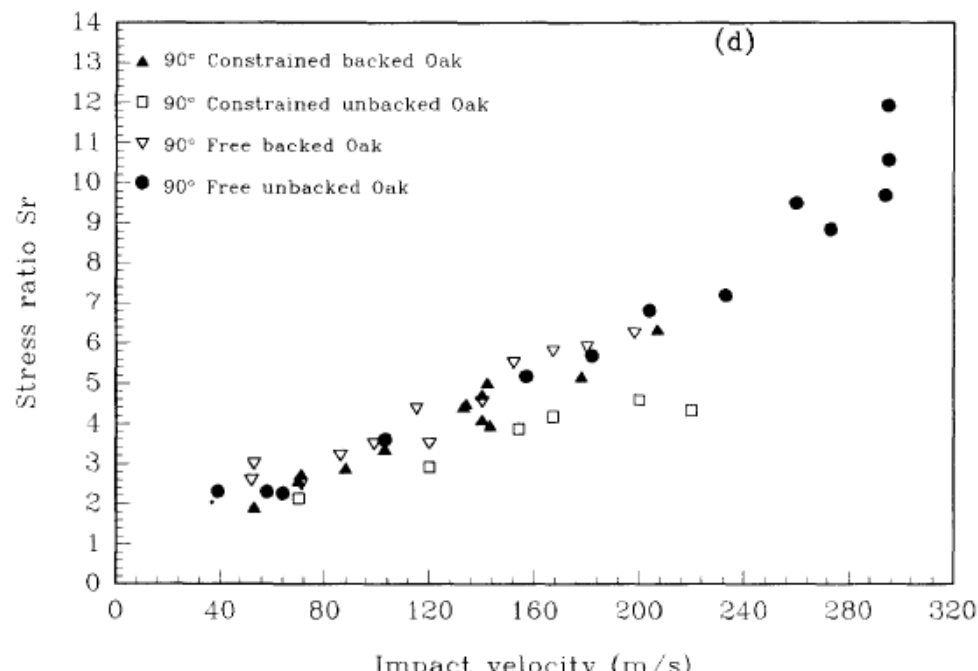
MPa

\* Free specimen.

Zgniatanie powolne

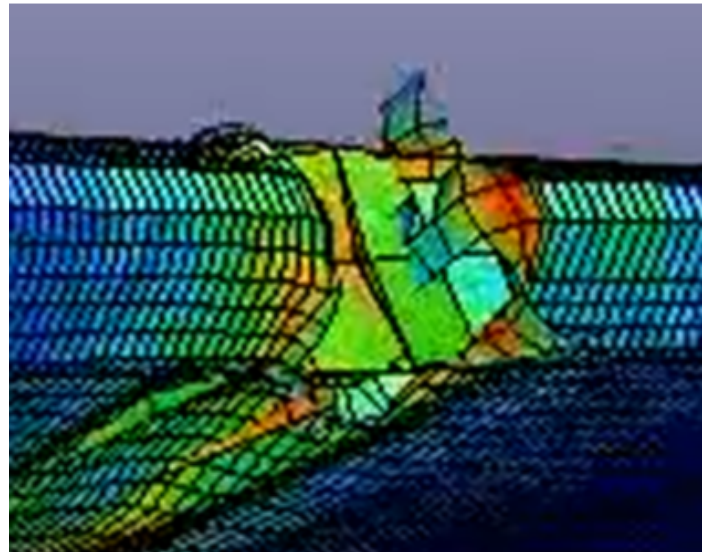
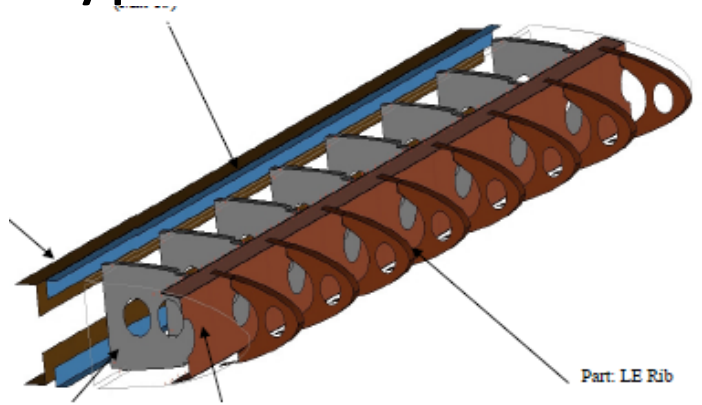


Rapidly crushed wood is much (~2 x) tougher than a slowly deformed wood.





# Modeling with LS-Dyna requires the knowledge of these typical issues with an FEM method



One of Binienda's models compared with a more realistic internal structure of the wing)

1. High resolution is a must
2. Beware of numerical erosion of FEM elements in dynamical situations. Conservation laws are violated if timber disappears, wing is not even challenged, tree inertia disappears
3. When time-step inexplicably drops to a rock-bottom value 1 ns in a low-res LS-Dyna sim (to cross 1 FEM tree cell the wing takes  $\sim 100000000$  time-steps!), the calculation is NOT accurate. It no longer makes sense. This could be due to excessive mesh distortion or hourglassing or something else.
4. Never overestimate the D16 alloy's thickness, especially by a factor of 3-4

there is one more thing – standard material models do not take this into account:

## Review on critical impact velocities in tension and shear

(they lower the toughness of J.R. Klepaczko aluminum alloys, and have been

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Available online 24 October 2005

exceeded in Smolensk)

### Abstract

J.R. Klepaczko / *International Journal of Impact Engineering* 32 (2005) 188–209

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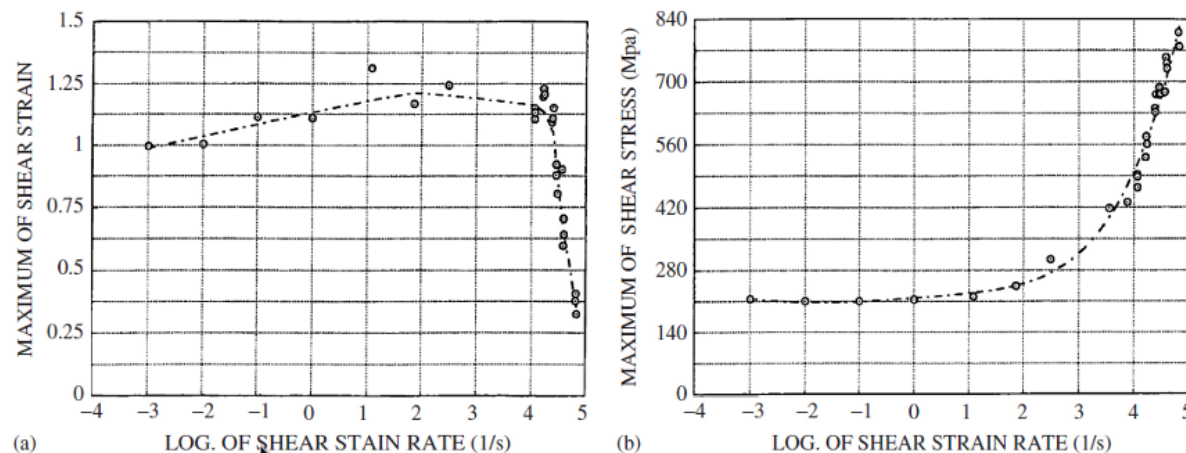


Fig. 15. Experimental results of slow and fast shearing for a hot rolled armor steel by the MDS technique: a—maximum shear strain at failure versus nominal strain rate; b—maximum shear stress versus nominal strain rate [10].

measured by the non-contact optical transducer 8 and by the black and white target 6. In addition, since the front of the striker is black the displacement of the contact striker-specimen can be also measured. The theory

Calculations of Binienda et al. (2012) – fully plastic tree (GHARD=0 !), totally unrealistic trunk bending

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**Lot Poziomy, Gęsta Siatka MES,  
Kąt Natarcia  $14^\circ$ , Mat143 oraz JC**

LEONA Keyword 143 by LE Praport  
Time 1: 1.00

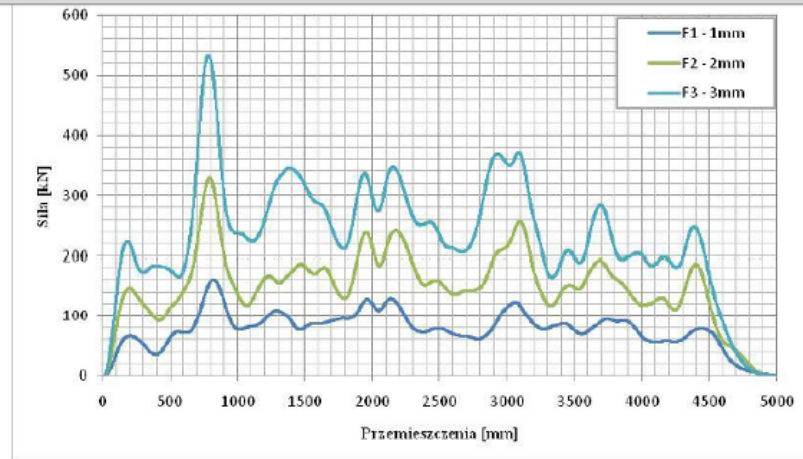
Spód skrzydła

# Example of correct usage of LS-Dyna:

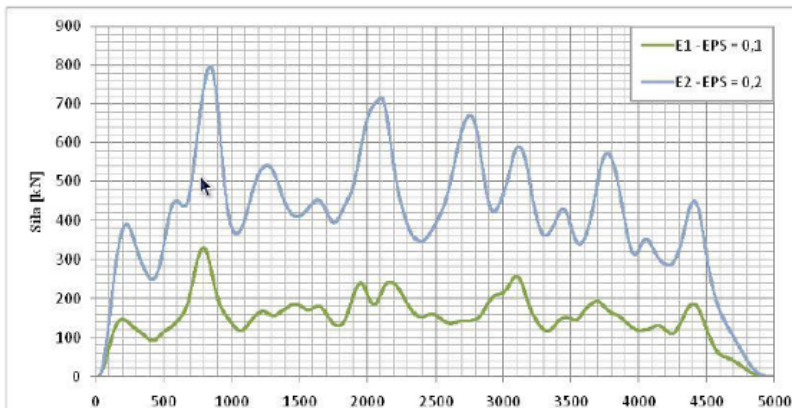
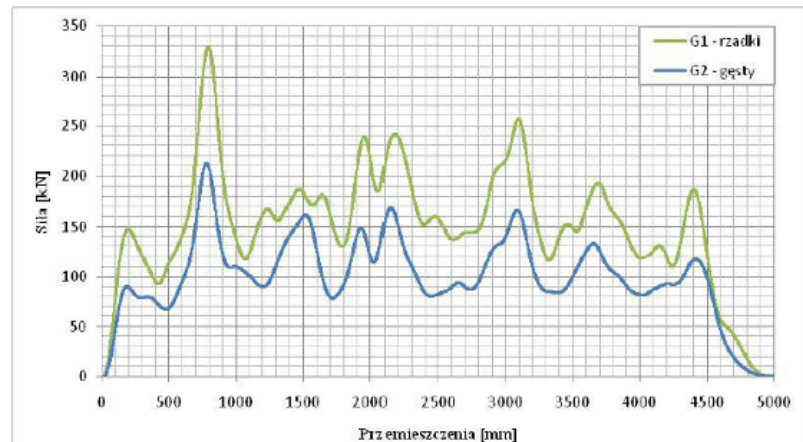
## A. Morka et al (2013)

drewna brzozy i stopu aluminium, odnalezienie danych nie było możliwe. Dlatego też zadano różne współczynniki tarcia ( $\mu=0,1$  oraz  $\mu=0,5$ ). W wariantach H1 oraz H2 przyjęto otwory w uźebrowaniu, grubość ścianki 2mm oraz  $EPS=0,1$ . Wykresy na Rys. 13 dają zbliżone wyniki. Oznacza to, że w procesie niszczenia tarcie pełni rolę drugoplanową.

Pomimo obecności perforacji w żebrach, na których rozpięto poszycie skrzydła, z dokumentacji trudno określić ich faktyczne gabaryty. Ponieważ do określenia wymiarów otworów użyto jedynie prostej proporcji, model poddano badaniu pod kątem zależności siły w miejscu kontaktu od ich średnicy. Zastosowano dwa zupełnie skrajne przypadki, pierwszy, w którym otwory są obecne oraz drugi, w którym nie występują. Wykres na Rys. 14. wykazuje pewne różnice w wielkości siły, jednak nie są one znaczące. Ponieważ wątpliwa jest jedynie kwestia wielkości i usytuowania perforacji żeber, a nie ich obecność można wnioskować, że model nie jest wrażliwy na te uproszczenia.

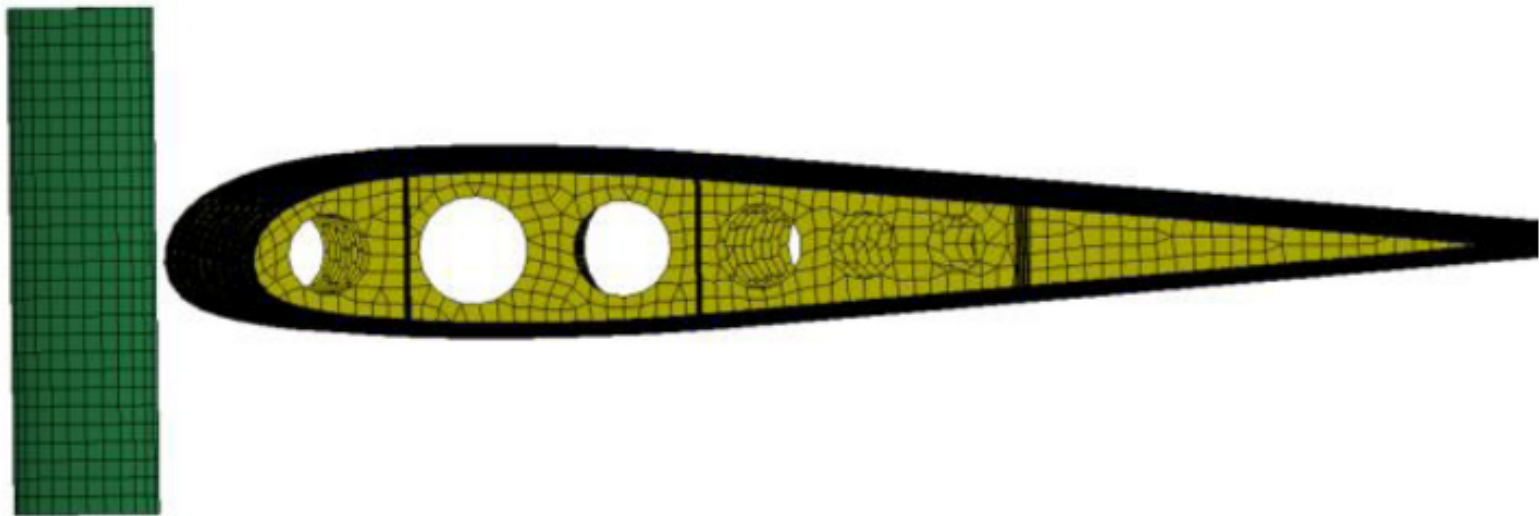


Rys. 11. Zależność siły oddziaływania skrzydła na belkę penetrującą w funkcji jej przemieszczenia dla trzech grubości struktury





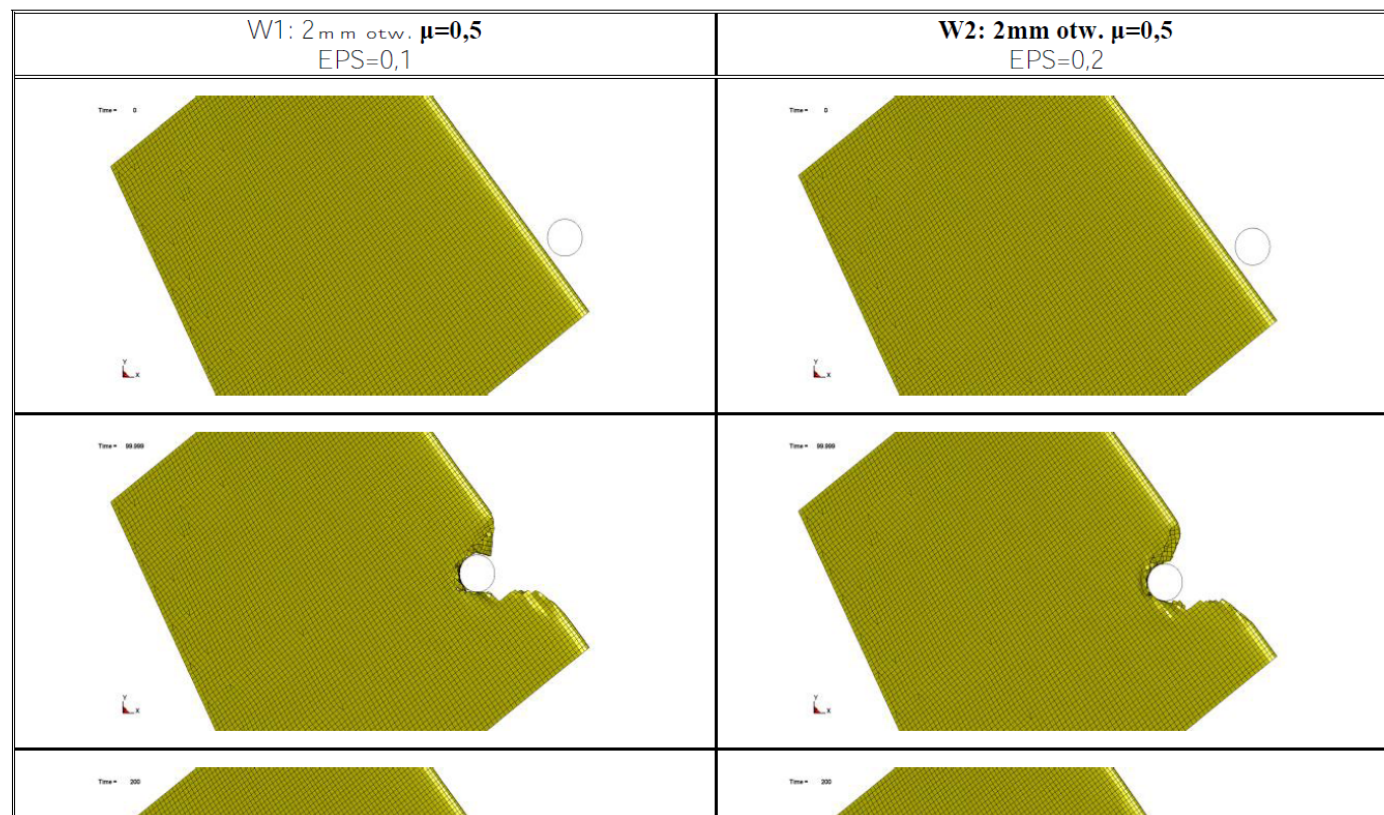
Morka et al (2012) = correct  
geometry of the wing



R<sub>ys.</sub> 8. Model skrzydła z zastosowaniem perforacji żeber

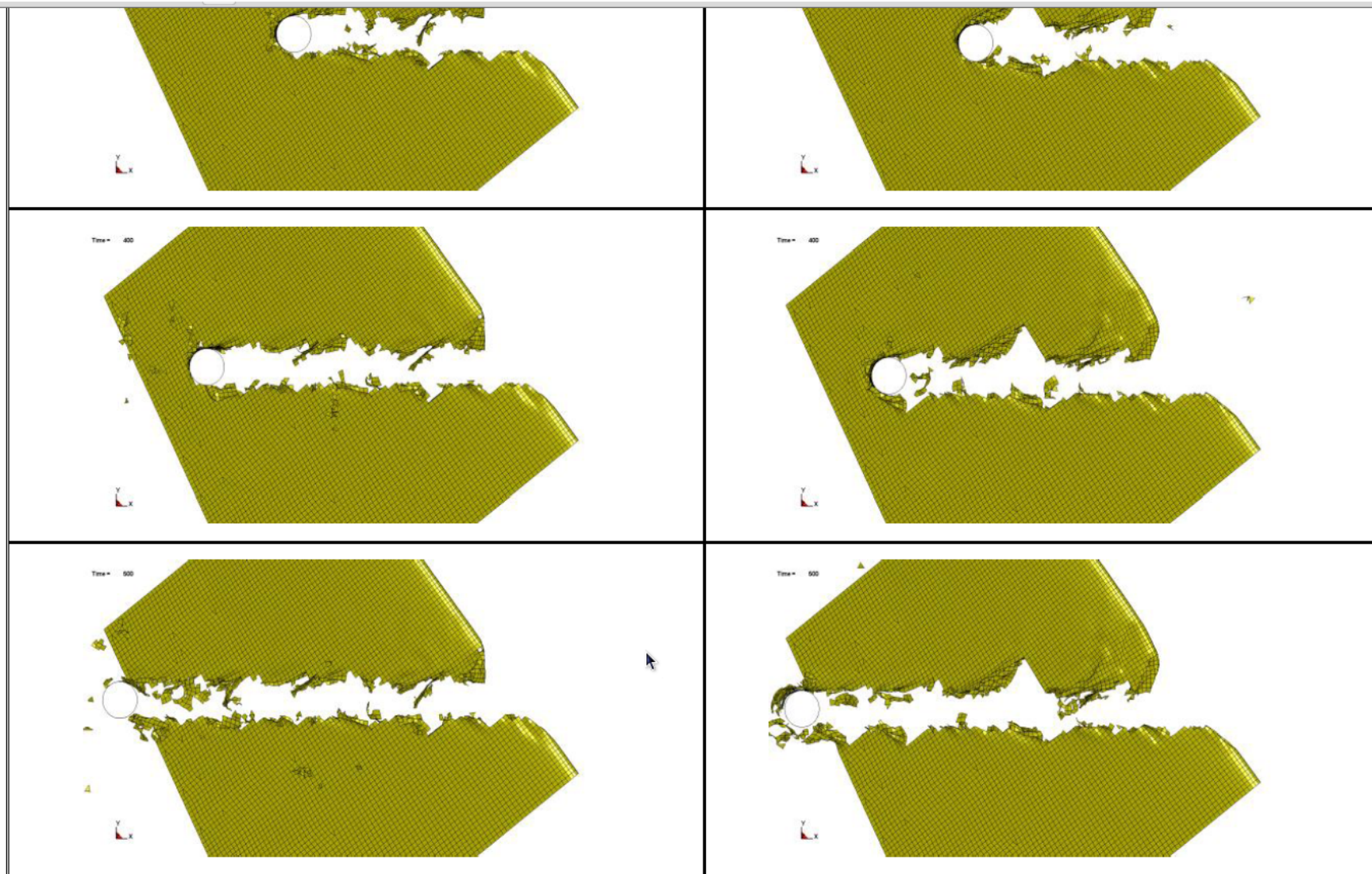
# Wing is cut by an undeformable cylinder in LS-Dyna (Morka et al. 2013)

## PROBLEMY MODELOWANIA NUMERYCZNEGO ZAGADNIENIA ZDERZEŃ CIAŁ





# Cutting the wing in LS-Dyna (Morka et al. 2013)

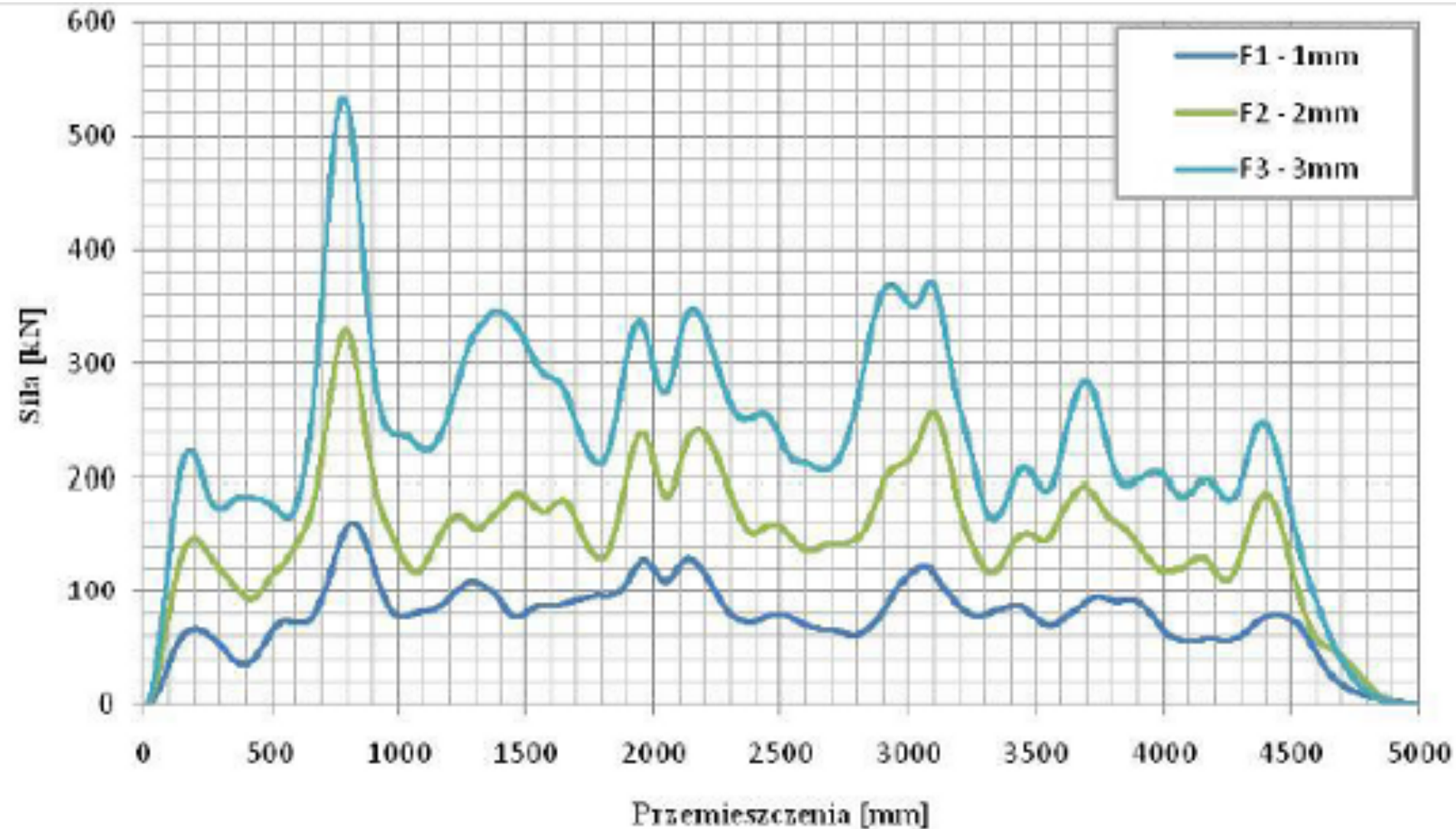


Rys. 9. Deformacja i niszczenie skrzydła dla dwóch wielkości zastępczego odkształcenia niszczącego w kolejnych chwilach czasu.

**T<sub>ab.</sub> 6. Wyniki testów wariantowych dla różnych wartości parametrów**

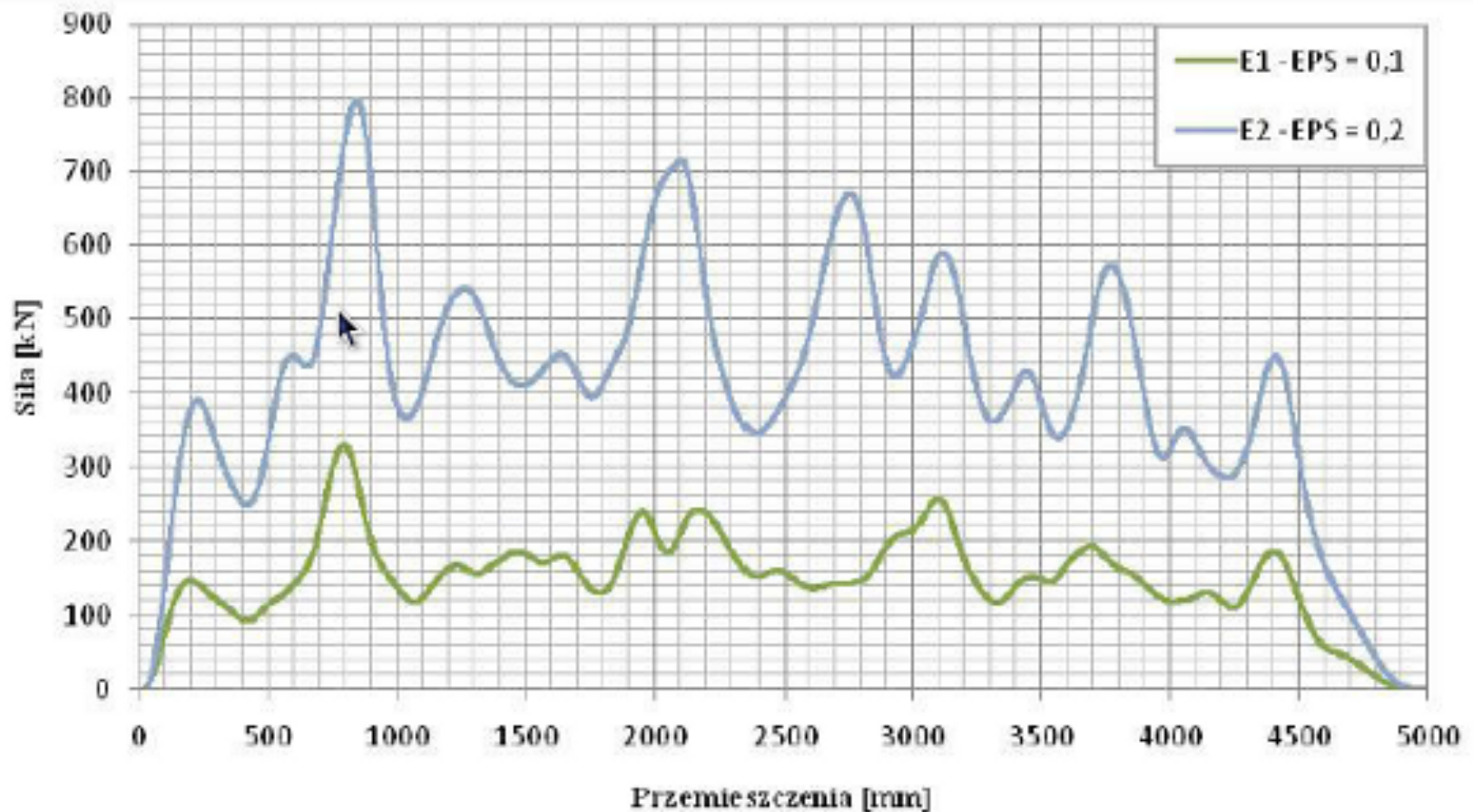
	force	aver. force
simulation parameters, thickness of metal sheets etc.	<b>Siła</b> maksymalna [kN]	<b>Siła średnia</b> [kN]
1mm $\mu=0,5$ EPS=0,1	163	79,3
2mm $\mu=0,5$ EPS=0,1	374,3	172,1
3mm $\mu=0,5$ EPS=0,1	611,9	248,1
1mm otw. $\mu=0,5$ EPS=0,1	161,5	77,3
2mm otw. $\mu=0,5$ EPS=0,1	329,8	149,9
3mm otw. $\mu=0,5$ EPS=0,1	534,3	231,2
2mm otw. $\mu=0,5$ EPS=0,2	797,1	407,3
2mm otw. $\mu=0,1$ EPS=0,1	435,4	164,8
1mm gęsty $\mu=0,5$ EPS=0,1	144,8	54,2
2mm gęsty $\mu=0,5$ EPS=0,1	274,6	127,2
3mm gęsty $\mu=0,5$ EPS=0,1	418,3	190,4
1mm otw.gęsty $\mu=0,5$ EPS=0,1	121,7	49,8
2mm otw. gęsty $\mu=0,5$ EPS=0,1	212,6	99,5
3mm otw. gęsty $\mu=0,5$ EPS=0,1	362,9	163,9

# Force as a function of displacement, for different mean aluminum alloy thicknesses



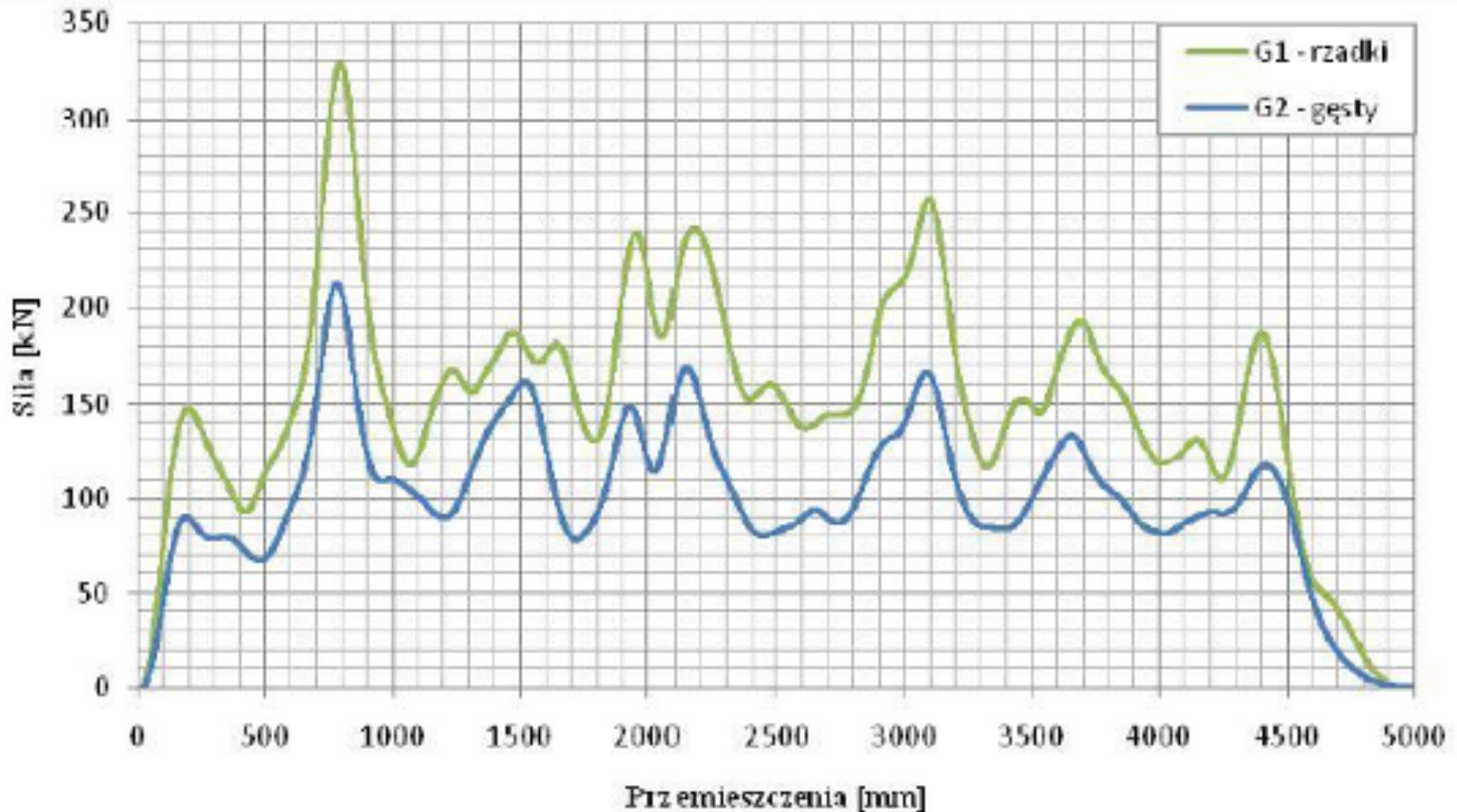


# How max. deformation parameters influence the wing-tree force.





Influence of the resolution of the mesh (green is sparse grid, blue is dense grid)



# CALCULATIONS OF TREE BREAKING

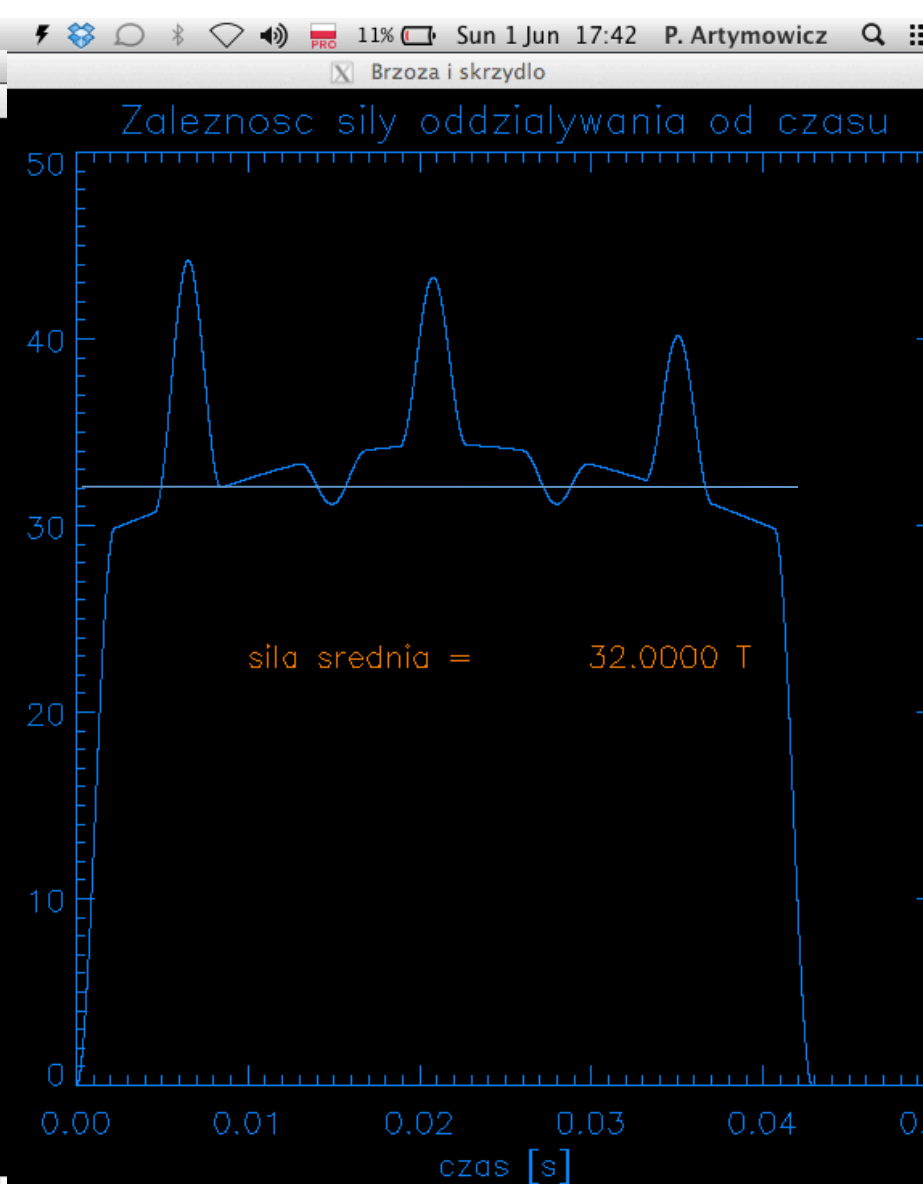
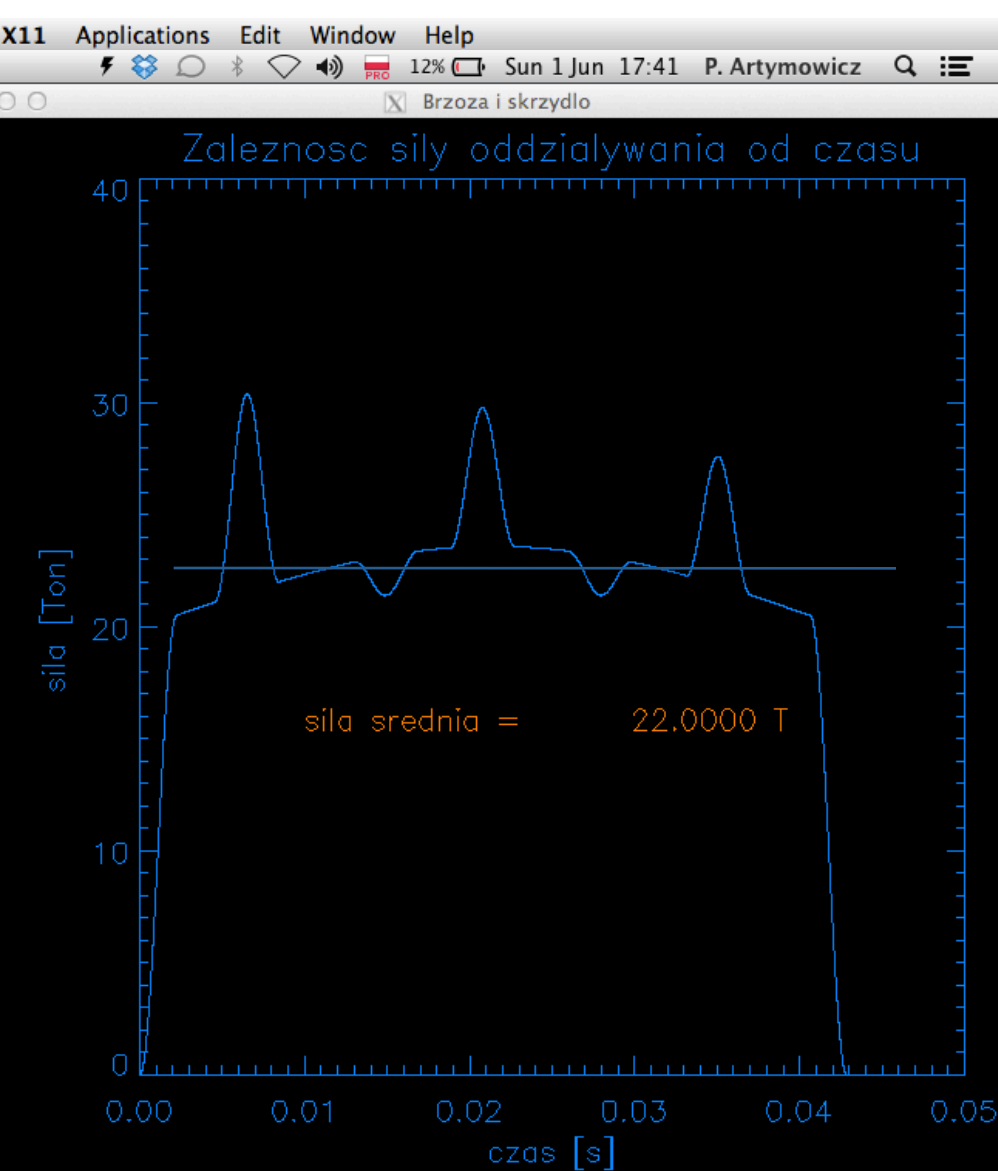
- Essential variable: the total force of tree-wing contact
- Realistic force in higher-resolution FEM equals 20-30 tonnes
- I will show the tree deformation calculations done in the IDL language
- Mathematical model: Timoshenko beam =
- Euler-Bernoulli beam generalized to include shear deformations and rotational inertia
- I further generalized that model to include axial strains and stresses, and a more tree-like, variable cross section

## Generalized TIMOSHENKO BEAM

$$m \frac{\partial^2 w}{\partial t^2} + \eta(x) \frac{\partial w}{\partial t} = \frac{\partial}{\partial x} \left[ \kappa A G \left( \frac{\partial w}{\partial x} - \varphi \right) \right] + q(x, t)$$
$$J \frac{\partial^2 \varphi}{\partial t^2} = N \frac{\partial w}{\partial x} + \frac{\partial}{\partial x} \left( E I \frac{\partial \varphi}{\partial x} \right) + \kappa A G \left( \frac{\partial w}{\partial x} - \varphi \right)$$

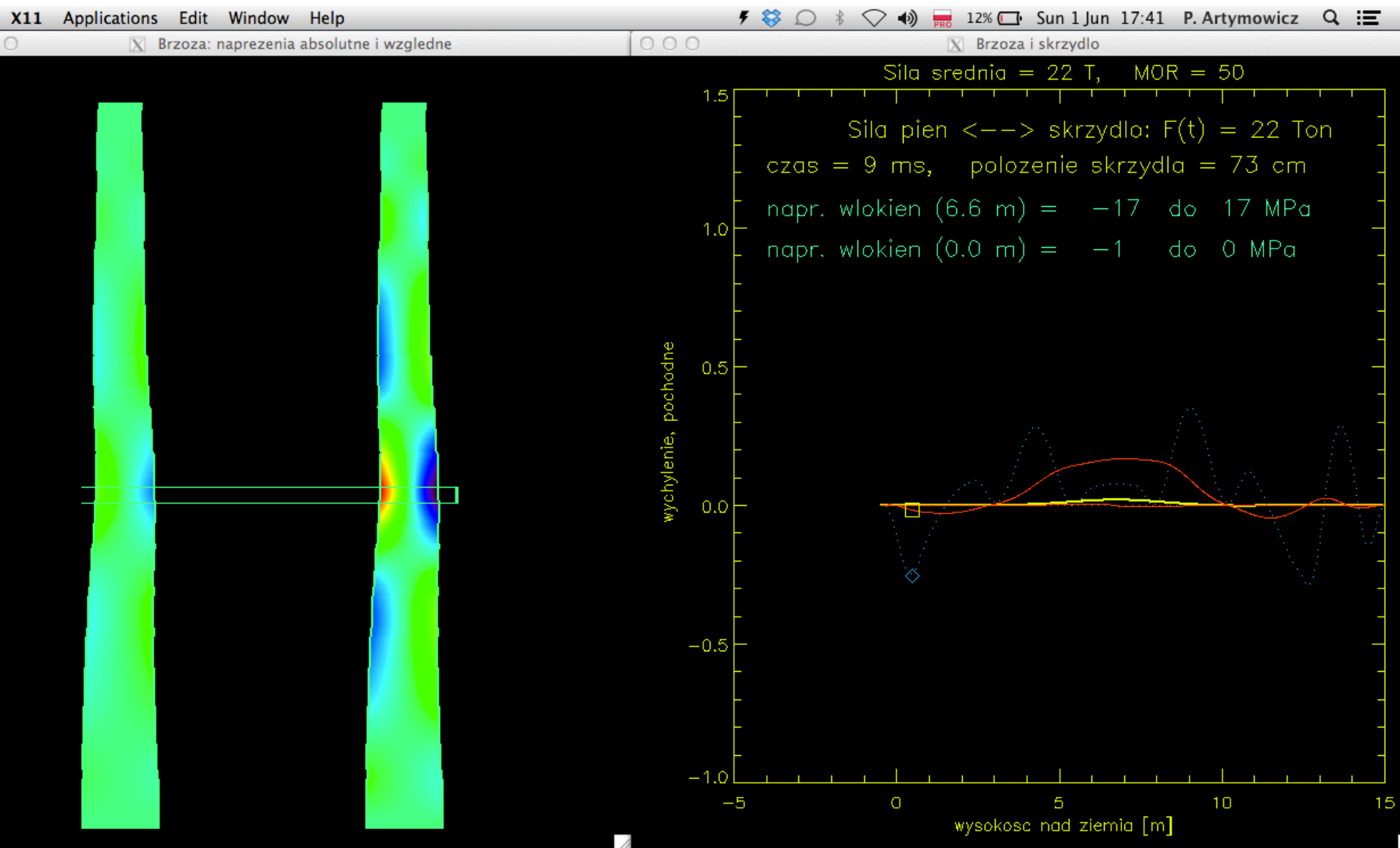
Model allows to study the deformations of elastic columns or beams subject to bending and shear, as well as additional axial loading such as the gravity of the beam. The above equations have been supplemented by axial motion equation, to take into account vertical component of deformation in a dynamic setting. The tree has a circular cross section and narrows from bottom to top.

# Time-variability of force (cf. Morka 2013) with the average 22 T and 32 T of force

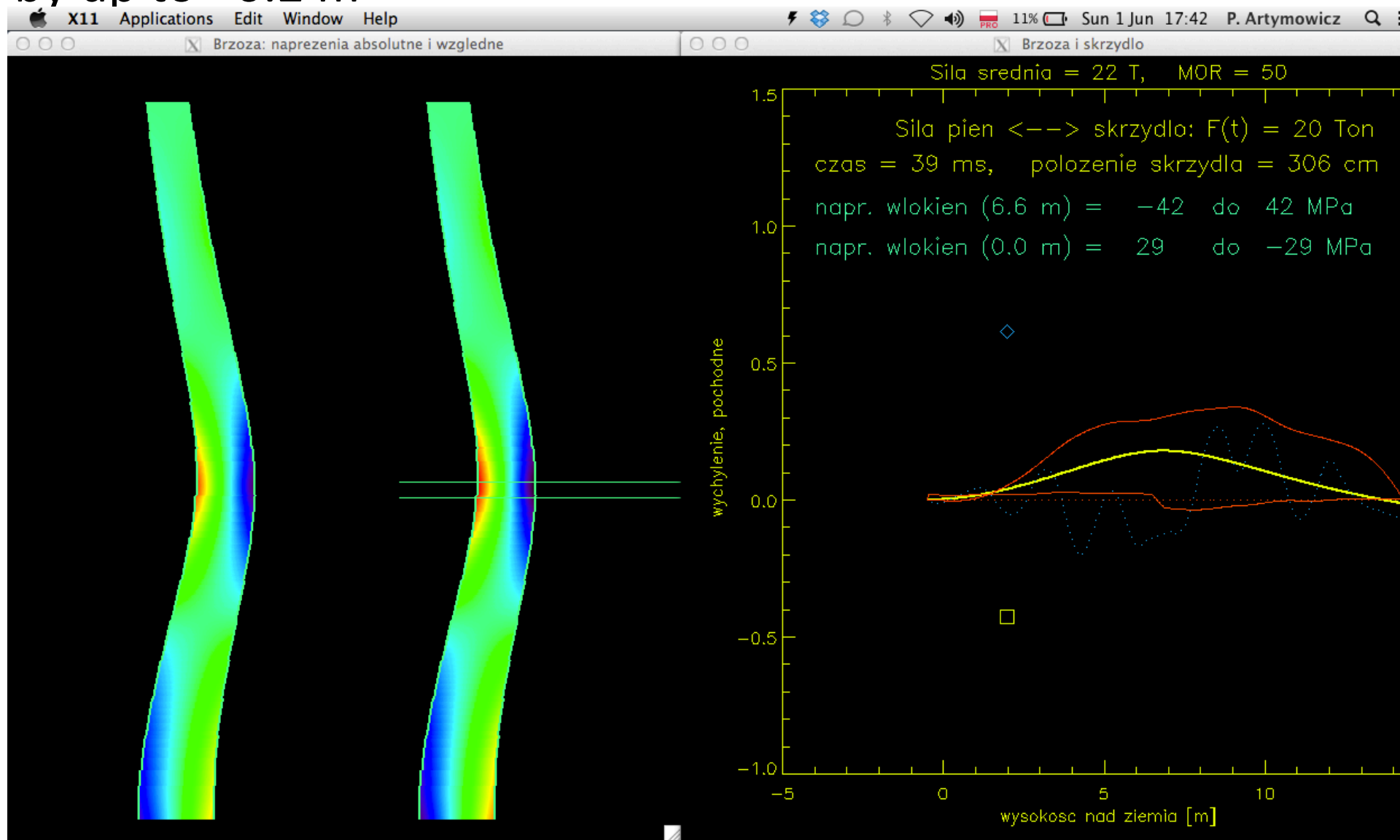




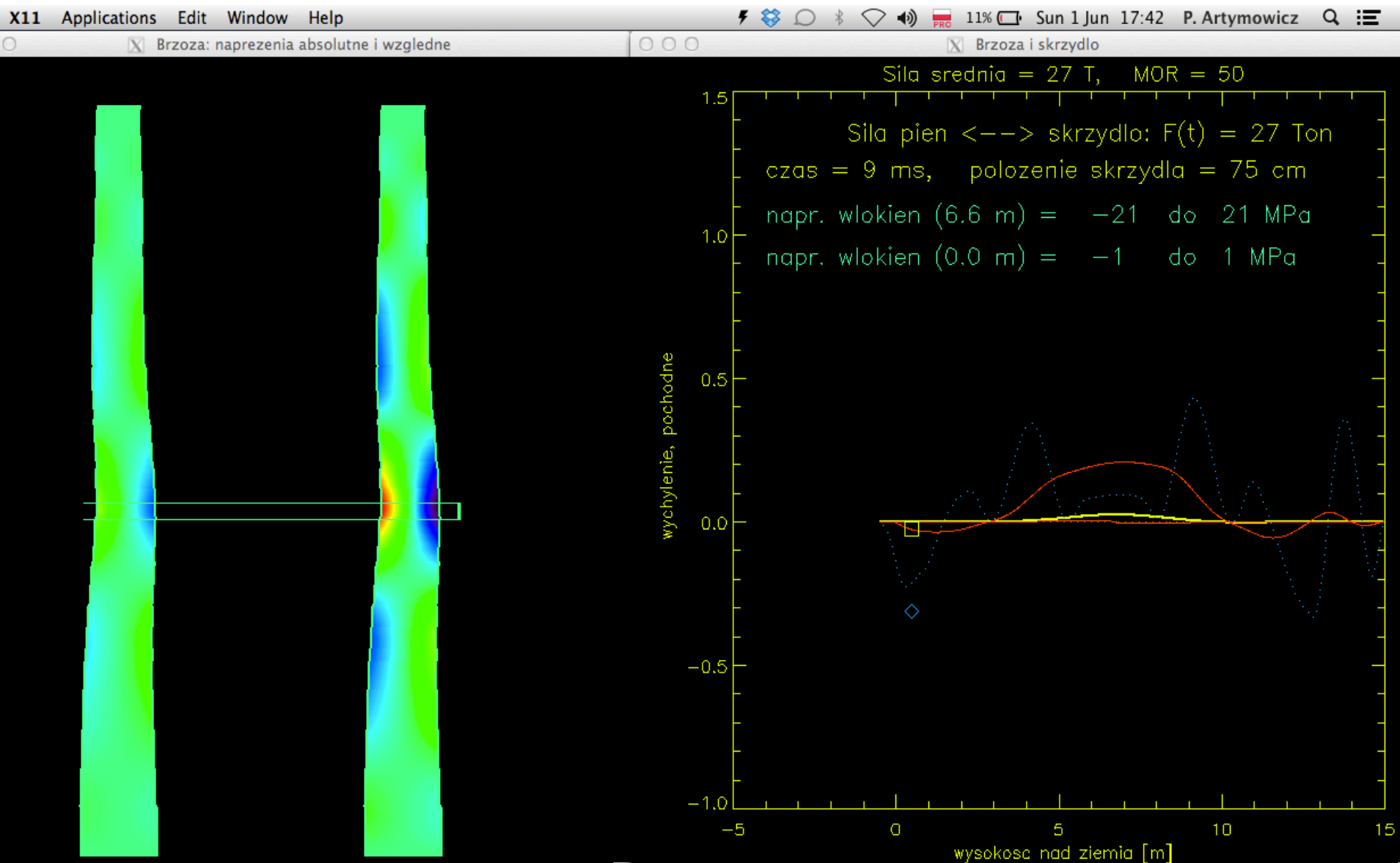
# Force 22 T, $t = 9$ ms, Map of absolute (left) and relative (right) axial stress on fibers



Force 22 T, time  $t = 39$  ms, stresses at 6.5m height =  $(\pm 42)$  in MPa. In this case there is no breakage; the trunk deflects by up to  $\sim 0.2$  m



# Force 27 T, time $t = 9$ ms

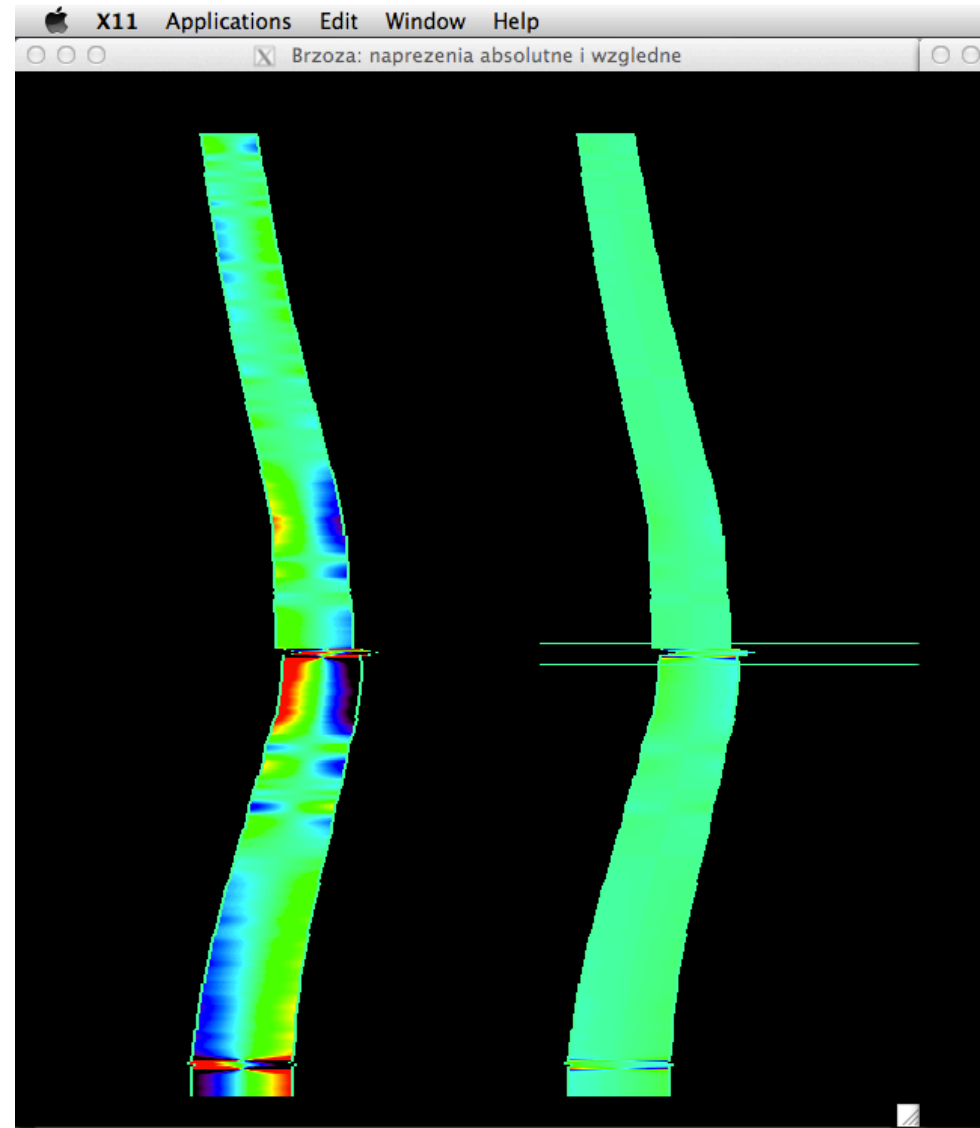


Force 27 T, time  $t = 23$  ms

Tension of fibers exceeds at the height of 6.5 m, as well as 0.6 m the limiting values (modulus of rupture for birch MOR  $\sim 50$  MPa).

A wavetrain of shear and dilatation waves is launched travels along the tree trunk.

(The fracture is not of a splinter type because of the low dimensionality of the Timoshenko beam model)



# Results

The tree trunk of the Bodin's birch modeled under realistically time-variable loading (the variability patterned after FEM calculations of Morka et al. 2012) with a mean force of 22 tonnes does not cause the breakage of the trunk

- Mean contact force of ~26 tonnes or larger causes fractures in the trunk (MOR is locally exceeded). The trunk is broken in two areas: one in the area hit by the wing and the other at the base near the ground, exactly as it happened in Smolensk in 2010. Mean force > ~30 ton (300 kN) requires too thick aluminum alloy sheets in the wing to be generated.
- The current model has reduced dimensionality and cannot answer all question, e.g. what is the deviation of the line of breakage of the wing from the direction of flight, what is the shape of fractures. Realistically they would have long splinters. More calculations are needed, although it seems conceivable that that the trunk hit by the delta-shaped wing, by deflects by the right amount to explain the small tilt of the cut line to the flightpath.



## Results

- In first approximation, an FEM simulation of the structure of the wing under collision with a tree can be done with a nondeformable obstacle, because the wing structural failure happens rapidly, in time when a large tree inertia excludes its rapid deformation. Such method was employed by the WAT research group of Morka et al.
- If however we want to reproduce the slightly slanted cut line of the wing (8 degrees w.r.t. flight direction) then we'd need to use a deformable trunk such as the one studied here, maybe also the small, planar wing distortion along its whole span. The task seems easy, since our  $\sim 0.5$  m bending corresponds to exactly such a slant angle given a  $\sim 3.5$  meter long chord of the wing.

## Results

- Destruction of a box structure of the wing always happens in correctly performed simulations
- Metal sheet thickness of order 2-3 mm leads to just enough loading on a 44 cm-diameter tree to cause its breakage. This happens long after the fate of the wing is already sealed: the breakage occurs when the wing is already largely cut off and it is leaving the area of interaction in two pieces.

## **Executive Summary:**

**(i) the problem of flight of the detached wingtip of the Smolensk Tupolev PLF 101, and  
(ii) the problem of the wing-tree collision  
have been solved.**

- Theoretical flight path of the 6.5-m part of the left wing agrees very well with the distance from the Bodin's birch tree to the place where it fell (110 m), and its very well-preserved state.
- The calculated, complex, tree breakage (at two different heights in the opposite directions) long after the initiation of wing destruction (under the mutual force of about 27-30 tonnes), is in a good agreement with the post-accident reports of Smolensk crash.